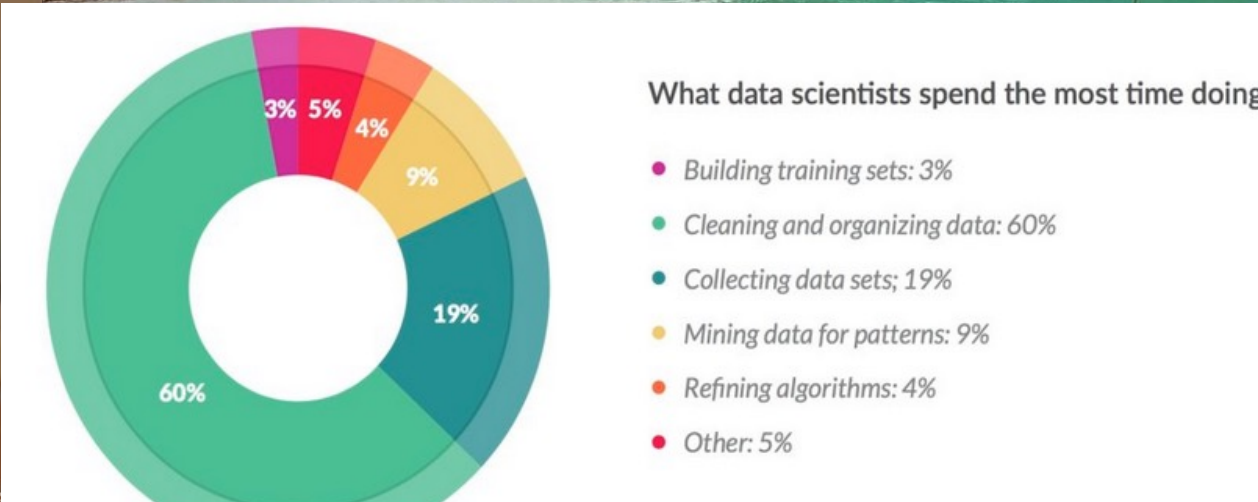


TU 257 – Fundamentals of Data Science

Data Analytics

L4 – Classification – Part 1

Brendan Tierney

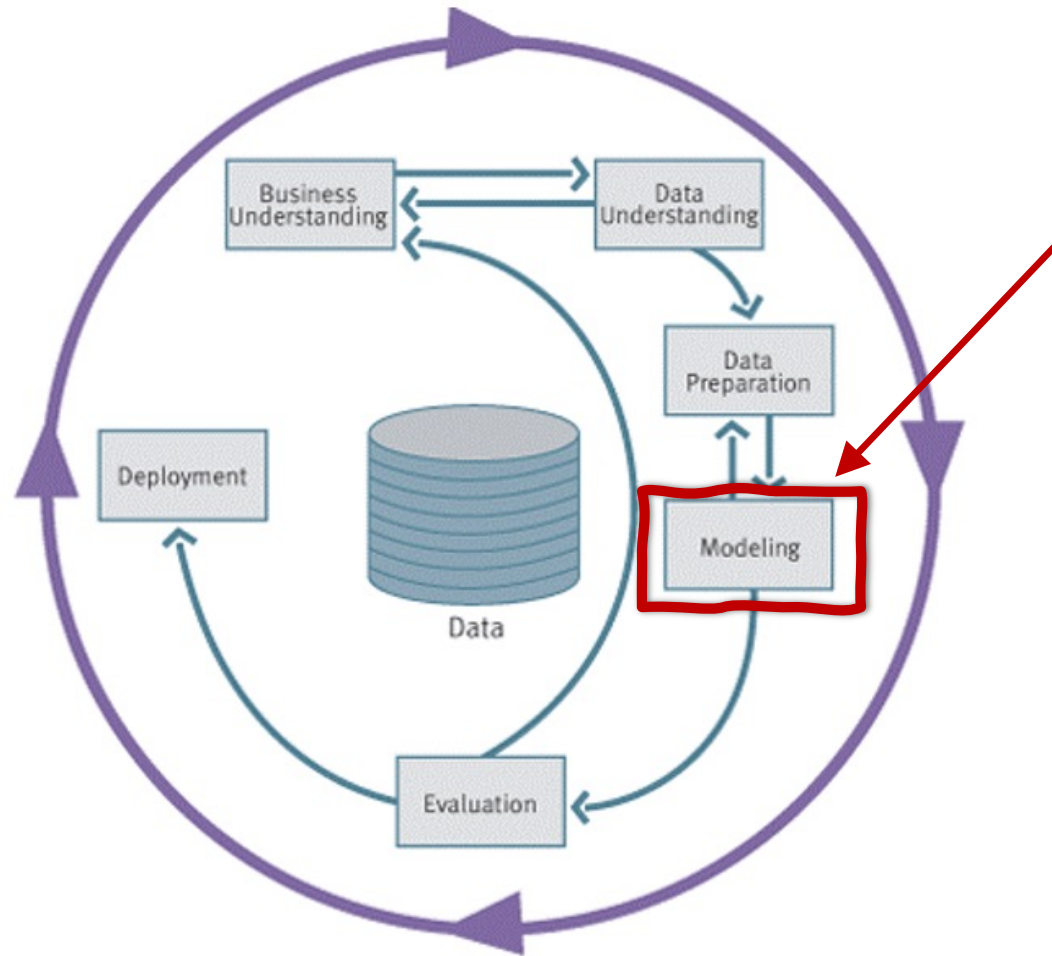


# Agenda

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- What is Classification
- What type of problems
- The Typical Process
- Preparing Data
- Lots of Algorithms
  - Subset this week
  - More next week
  - Not all will be covered
- Some details/background/under-the-hood at the algorithms
  - Inner details are not needed. Can be explored in a Machine Learning module
- How do you measure if it's any good

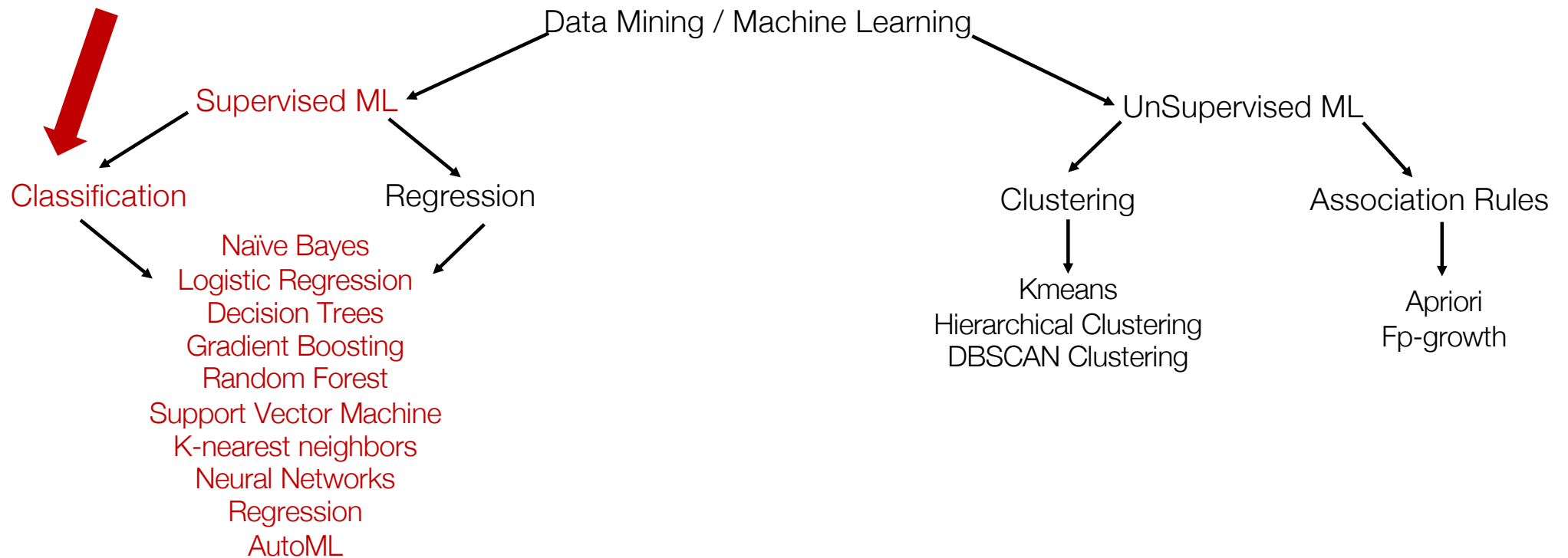


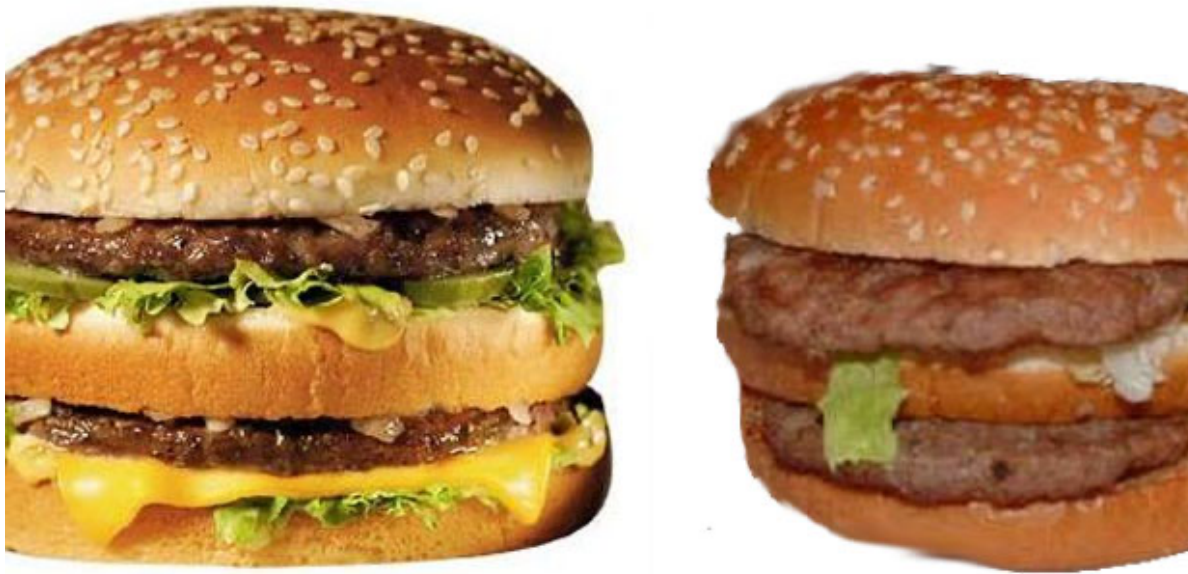


# Data Mining / Machine Learning

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- the use and development of computer systems that are able to learn and adapt without following explicit instructions, by using algorithms and statistical models to analyse and draw inferences from patterns in data.





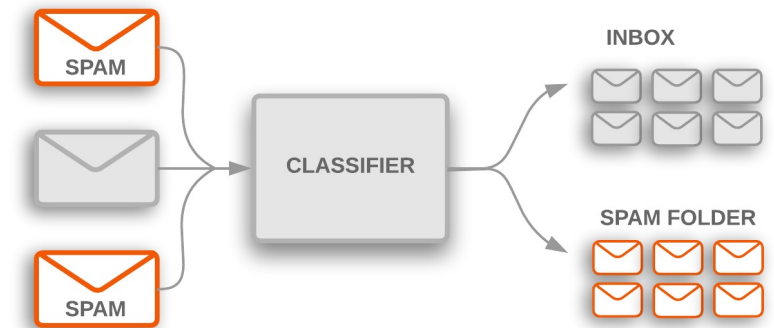
# theory **VS** reality

- Most Data Analytics etc can be done in a few lines of code
- Don't worry about the Theory, we might touch upon some of it, but it isn't necessary to know in-depth
- You'll never have to write an algorithm from scratch

# What is Classification

---

- **Classification** is a task that requires the **use of (machine learning) algorithms** that learn how to **assign a class label to examples** from the problem domain.
  - We learn from the past to predict the future
  - An easy to understand example is classifying emails as “*spam*” or “*not spam*.”



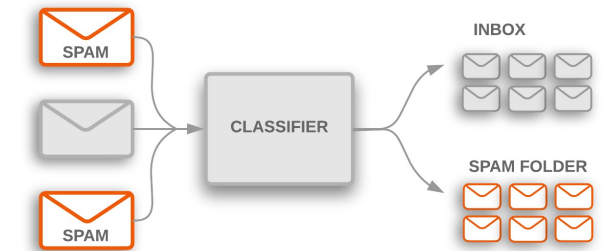
- Classification predictive modeling involves:
  - Looking at **historical data** representing a particular scenario
  - **Using algorithms to find patterns** in the data
    - What attributes/features contribute towards determining the scenario being investigated
    - **Assign a class label.**

# Classification – Different types

---

- **Binary classification** refers to predicting one of **two classes**

- Yes / No
- 0 / 1
- Buy / Not-Buy
- Spam / Not-Spam



- **Multi-class Classification** is when we have **more than two class values**

- Different Fruits
- Credit Ratings
- Different Products





# Classification: Definition

---

- Given a collection of records (*training set*)
  - Each record contains a set of *attributes*, one of the attributes is the *class*.
- Find a *model* for the class attribute as a function of the values of other attributes.
- Goal: previously unseen records should be assigned a class as accurately as possible.
  - A *test set* is used to determine the accuracy of the model. Usually, the given data set is divided into training and test sets, with training set used to build the model and test set used to validate it.

# Classification—A Two-Step Process

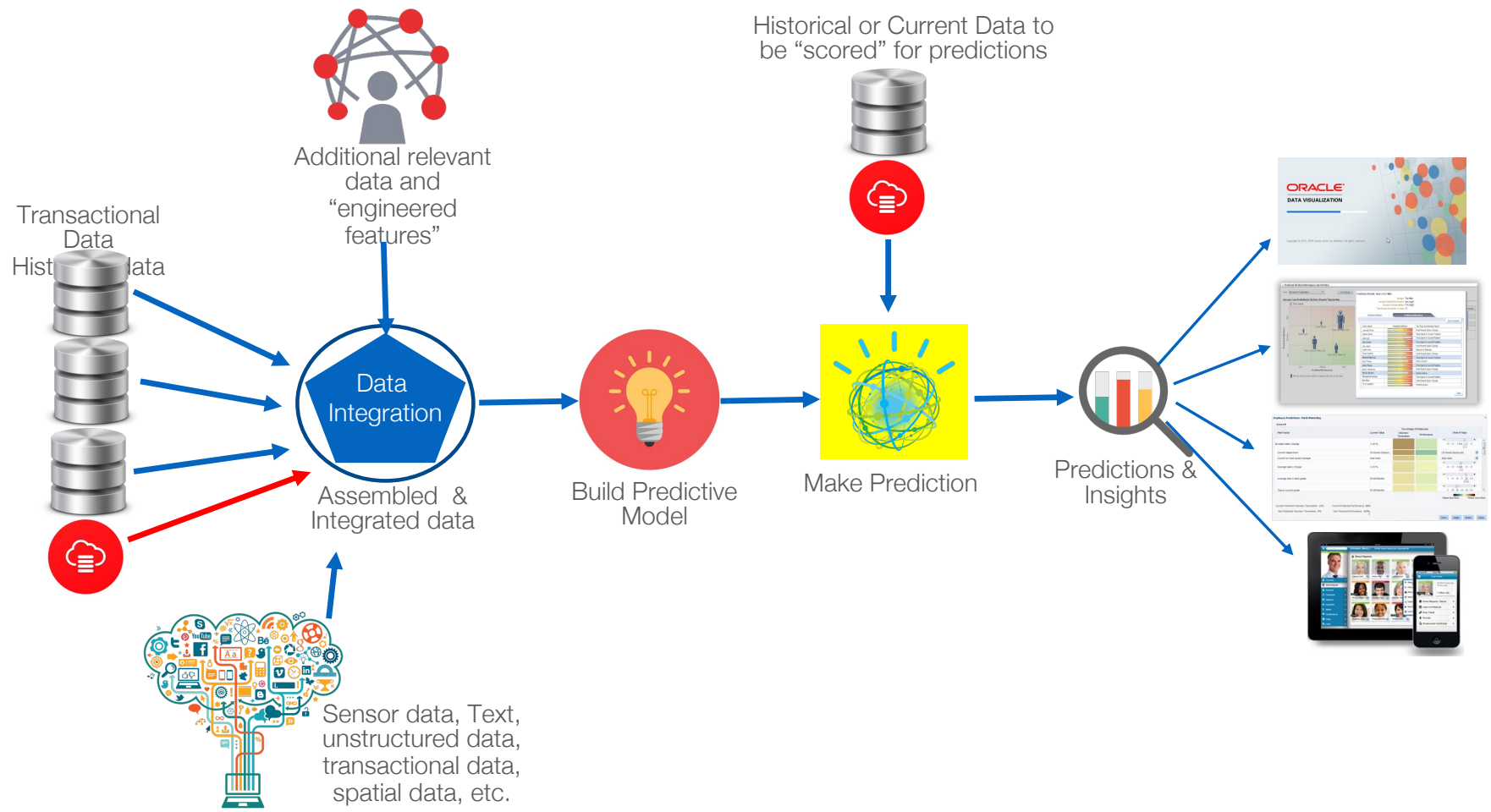
---

- **Step 1 - Model Construction:** describing a set of predetermined classes
  - Each tuple/sample is assumed to belong to a predefined class, as determined by the class label attribute
  - Create a sub-set of tuples to be used for model construction: training dataset
  - Create a models using different algorithms
    - Each algorithms takes the training dataset as input
- **Step 2 – Model Test & Evaluation**
  - The model is represented as classification rules, decision trees, or mathematical formulae
  - Estimate accuracy of the model
    - The known label of test sample is compared with the classified result from the model
    - Accuracy rate is the percentage of test set samples that are correctly classified by the model
    - Test set is independent of training set, otherwise over-fitting will occur

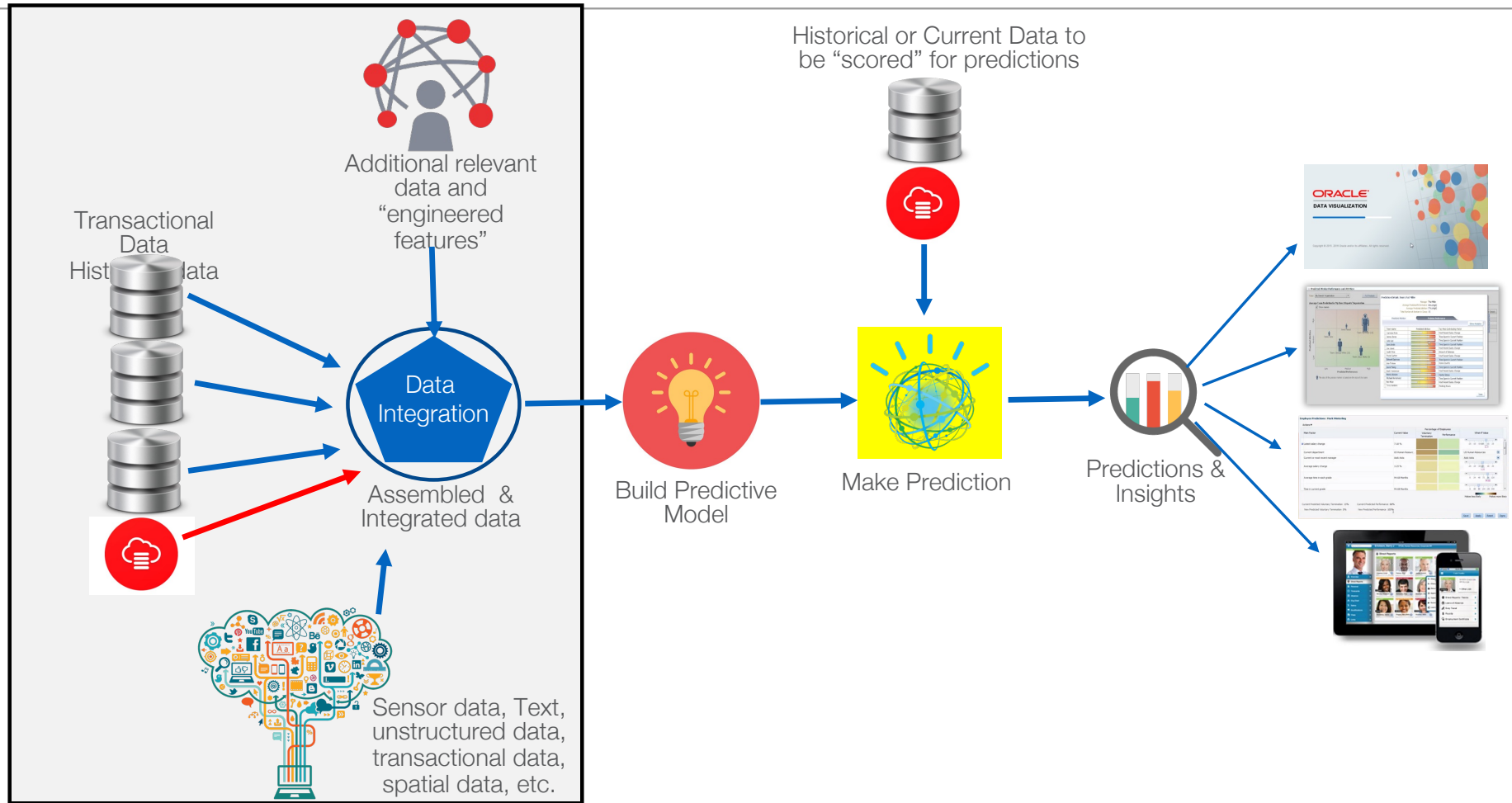
# Classification—A Two-Step Process or is it a Three Steps

---

- **Step 1 - Model Construction:** describing a set of predetermined classes
  - Each tuple/sample is assumed to belong to a predefined class, as determined by the class label attribute
  - Create a sub-set of tuples to be used for model construction: training dataset
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    - Each algorithms takes the training dataset as input
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    - Test set is independent of training set, otherwise over-fitting will occur
- **Step 3 – Using the Model on new data**
  - Put into production
  - Use on newly generated data
  - Need to constantly Review and assess if the model needs to be update
  - Iterative

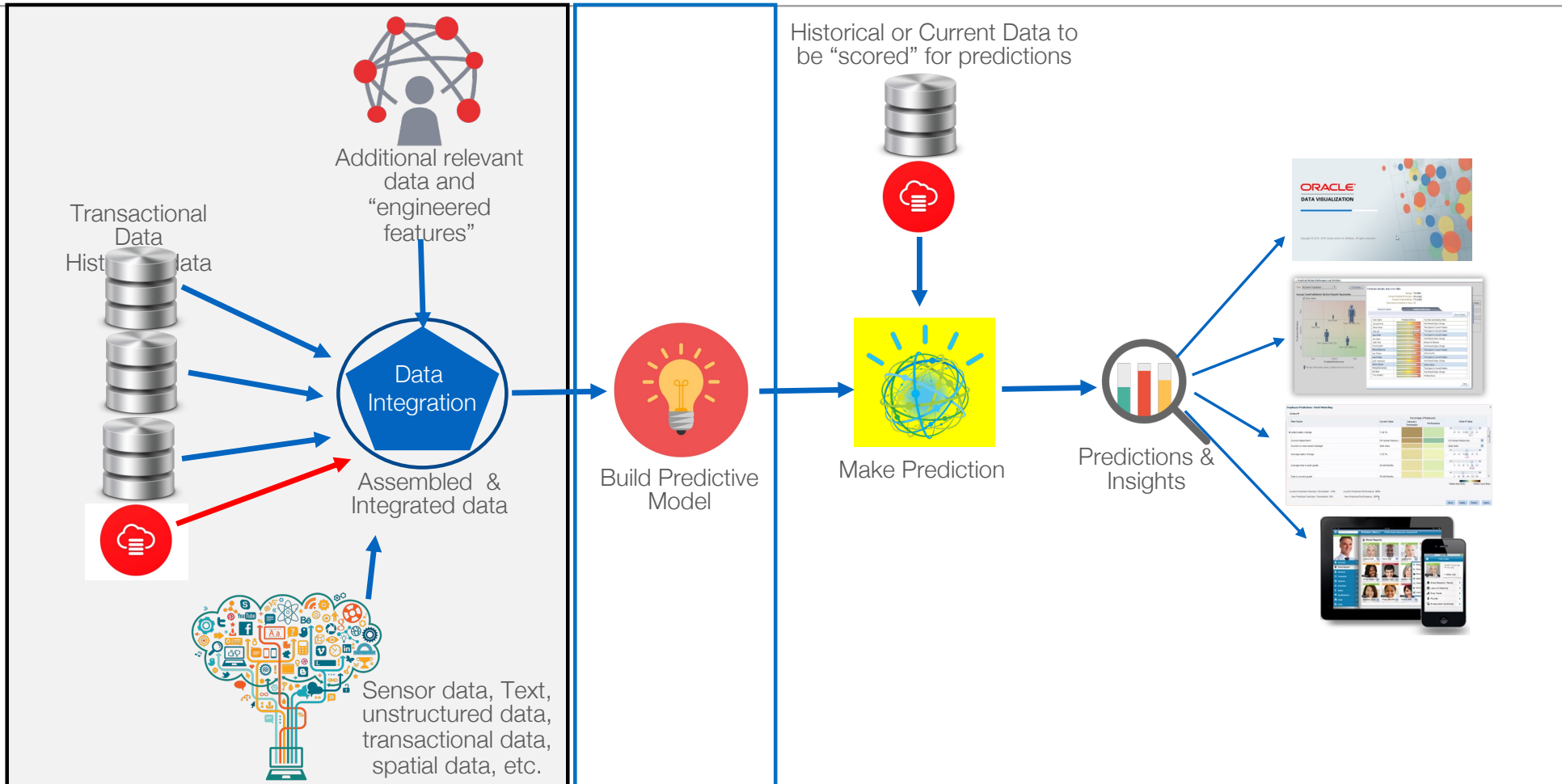


# Data Engineering



## Data Engineering

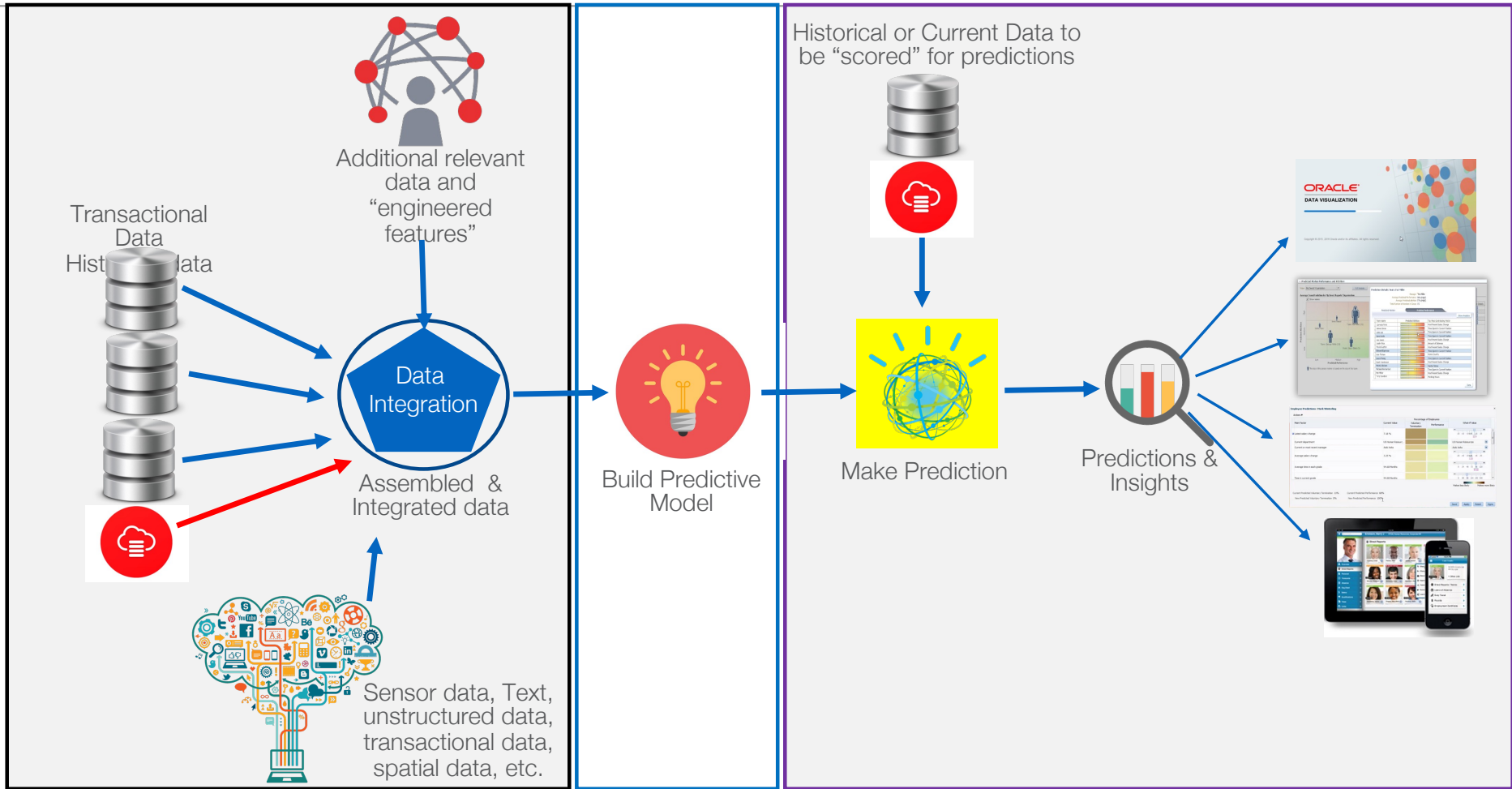
## Model Training & Evaluation



## Data Engineering

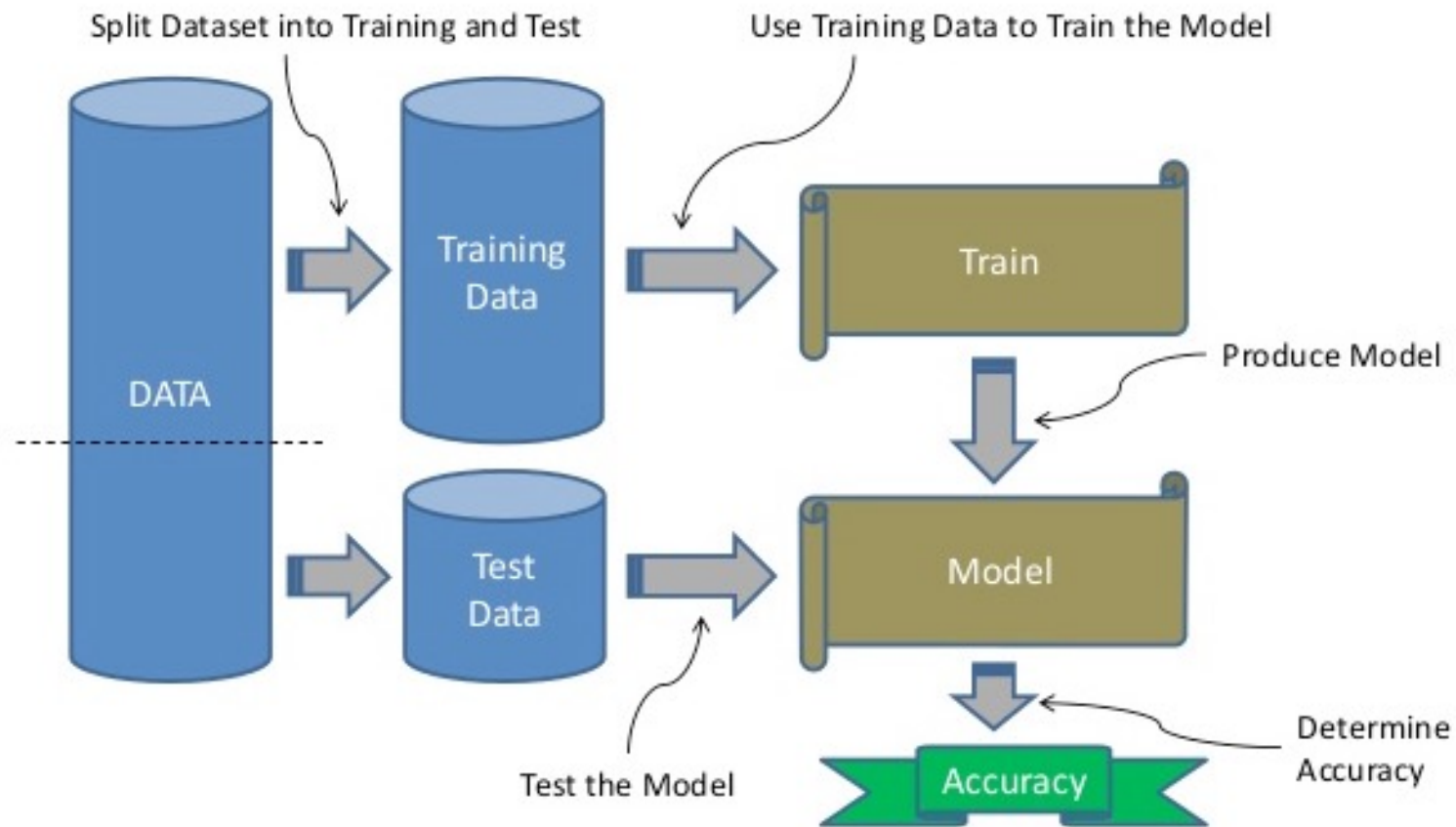
## Model Training & Evaluation

## Model Deployed in Production / MLOps



Data Set = Training + Test data sets

---





# The Algorithms

$\Sigma F_y = 0 \Rightarrow F_n - mg \cos \theta = 0$   
 $|F_n| = mg \cos \theta$   
 $\Sigma F_x = \max$   
 $M.R.L.u = \frac{mg \sin \theta \max}{mg \cos \theta \max} = \tan \theta \max$   
 $F_{R, \max} = -M.R.L.u \cdot mg \cos \theta = 0$   
 $= -mg \sin \theta \max$

$E_{pot, A} = 0$   
 $E_{kin, A} = 0$   
 $F = m \cdot g + 2F_s$   
 $a = \frac{dv}{dt} = \frac{dv}{du} \frac{du}{dt}$   
 $= \frac{(m_2 - m_1)g}{(m_1 + m_2)}$   
 $v = \sqrt{\frac{2(m_2 - m_1)gl}{(m_1 + m_2)}}$   
 $\frac{1}{2}mv^2 + mgy = \frac{1}{2}mv^2 + mgy$

$\lambda = \frac{v}{f}$   
 $\omega = 2\pi f$   
 $y(x,t) = A \sin(2\pi \frac{x}{\lambda} + t)$   
 $y(x,t) = A \sin(kx - \omega t)$   
 $2\pi v = k \omega = \frac{2\pi}{\lambda} v$   
 $\lambda_{max} = 2.99 \text{ mm}$   
 $P_e = e \sigma A T^4$   
 $P_a = e \sigma A T_0^4$   
 $\Delta P = e \sigma A (T^4 - T_0^4)$

$\Psi = 0, d = n \frac{2\pi}{\lambda}; n = 1, 2, 3$   
 $E = \frac{1}{2}mv^2 = \frac{p^2}{2m}; E_n = \frac{p_n^2}{2m}$   
 $E_3 = 9E_1$   
 $E_2 = 4E_1$   
 $E_1 = \frac{h^2}{8md^2}$   
 $n v = |E - E_1|$

$dE_1 = \frac{1}{4\pi \epsilon_0} \frac{dq}{r^2}$   
 $dE_2 = \frac{2}{4\pi \epsilon_0} \frac{dx}{r^2}$   
 $dE_3 = \frac{2}{4\pi \epsilon_0} \frac{y dx}{r^2}$

$\lambda_1 = \frac{u_1}{f}; \lambda_2 = \frac{u_2}{f}$   
 $\sin \theta_2 = \frac{\lambda_1}{\lambda_2} \sin \theta_1$   
 $\frac{\sin \theta_2}{\sin \theta_1} = \frac{\lambda_1}{\lambda_2} = \frac{u_1}{u_2}$   
 $\frac{v_1 \sin \theta_2}{v_2 \sin \theta_1} = \frac{v_1}{v_2} = \frac{u_1}{u_2}$   
 $\frac{v_1}{v_2} = \frac{u_1}{u_2}$

$\Psi(x,0) = A \exp(-\frac{x^2}{2\sigma_x^2}) e^{i k x}$   
 $|\Psi|^2 = A^2 \exp(-\frac{x^2}{\sigma_x^2})$   
 $B(k) = \frac{\sqrt{\sigma_x}}{\sqrt{\pi}} e^{-\sigma_x^2(k-k_0)^2}$   
 $\text{Re}(\Psi) = A \cos(k_0 x - \omega t)$   
 $|F| = \frac{1}{4\pi \epsilon_0} \frac{ze^2}{r^2} = \frac{mv^2}{r}$   
 $E_{pot} = -\frac{1}{4\pi \epsilon_0} \frac{ze^2}{r}$   
 $E_{kin} = \frac{1}{2}mv^2 = \frac{1}{2} \frac{1}{4\pi \epsilon_0} \frac{ze^2}{r}$   
 $E_{pot} = -2E_{kin}$

$U_H = -\int \mathbf{J} \cdot (\frac{\mathbf{V}}{c}) d\mathbf{e}$   
 $U_H = E_H b = v d b b$   
 $\mathbf{J} = \frac{1}{V} q \mathbf{v} dA$   
 $\frac{1}{V} = \frac{1}{A_1 b} = \frac{1}{A_2 b}$   
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 $= \frac{1}{4\pi \epsilon_0} \frac{ze^2}{r}$   
 $A'B' = \frac{s'}{s}$   
 $\frac{A'B'}{PO} = \frac{s' - \frac{1}{2}}{\frac{1}{2}}$   
 $\frac{s'}{s} = \frac{s' - \frac{1}{2}}{\frac{1}{2}}$

$v_1 \rightarrow v_2 = m_1 v_1 + m_2 v_2$   
 $\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$   
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 $F_s = \frac{m_1 a}{\cos \theta}; |F_s| = \frac{\max}{\sin \theta}$

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# The Algorithms

---

- This week
  - Naive Bayes
  - Decision Trees
  - Random Forests
  - XGBoost

- Other algorithms next week





**Essentially, all models are wrong, but some are useful**

**George Box**

A model is a simplification or approximation of reality  
and hence will not reflect all of reality.

His paper was published in the *Journal of the American Statistical Association*, 1976  
Book *Empirical Model-Building and Response Surfaces*, 1987

# The Algorithms

Naive Bayes

Decision Trees

Random Forests

XGBoost

The image contains a comprehensive set of handwritten physics notes. Key sections include:

- Mechanics:** Newton's laws on an inclined plane, conservation of energy ( $E_{pot} = mgh$ ), momentum, and circular motion.
- Electromagnetism:** Electric field calculations for point charges and dipoles, magnetic field, and energy density.
- Waves:** Sinusoidal wave functions, wave speed, and energy transport.
- Optics:** Ray diagrams for lenses and mirrors, and interference patterns.
- Mathematics:** Various calculus derivations, including the chain rule and integration techniques.

# Naïve Baye

---

- **Naive Bayes** is a probabilistic classifier in Machine Learning which is built on the principle of **Bayes theorem**.
- Naive Bayes classifier **assumes that one particular feature** in a class **is unrelated to any other feature** and that is why it is known as naïve
  - It is based on probability models that incorporate strong independence assumptions.
  - The independence assumptions often have little impact on reality. Therefore they are considered as naïve.

- Sounds Complicated!

- 1786!

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

↑ THE PROBABILITY OF "A" BEING TRUE GIVEN THAT "B" IS TRUE

↓ THE PROBABILITY OF "B" BEING TRUE GIVEN THAT "A" IS TRUE

↪ THE PROBABILITY OF "A" BEING TRUE

↩ THE PROBABILITY OF "B" BEING TRUE

# Naïve Baye

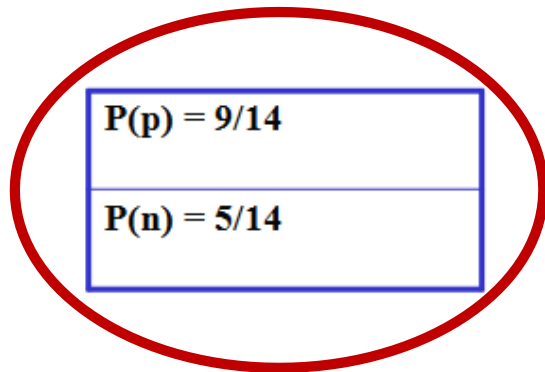
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- Naive Bayes classifier calculates the probability of an event in the following steps:
  - Step 1: Calculate the **prior probability** for given class labels
  - Step 2: Find **Likelihood probability** with **each attribute** for each class
  - Step 3: Put these values in Bayes Formula and **calculate posterior probability**.
  - Step 4: See **which class has a higher probability**, given the input belongs to the higher probability class.
  
- **Let's look at an example**

# Play-tennis example: estimating $P(x_i|C)$

---

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
rain	mild	high	false	P
rain	cool	normal	false	P
rain	cool	normal	true	N
overcast	cool	normal	true	P
sunny	mild	high	false	N
sunny	cool	normal	false	P
rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N



$P(p) = 9/14$
$P(n) = 5/14$

# Play-tennis example: estimating $P(x_i|C)$

Outlook	Temperature	Humidity	Windy	Class
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sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N

$P(p) = 9/14$
$P(n) = 5/14$

outlook	
$P(\text{sunny} p) = 2/9$	$P(\text{sunny} n) = 3/5$
$P(\text{overcast} p) = 4/9$	$P(\text{overcast} n) = 0$
$P(\text{rain} p) = 3/9$	$P(\text{rain} n) = 2/5$
temperature	
$P(\text{hot} p) = 2/9$	$P(\text{hot} n) = 2/5$
$P(\text{mild} p) = 4/9$	$P(\text{mild} n) = 2/5$
$P(\text{cool} p) = 3/9$	$P(\text{cool} n) = 1/5$
humidity	
$P(\text{high} p) = 3/9$	$P(\text{high} n) = 4/5$
$P(\text{normal} p) = 6/9$	$P(\text{normal} n) = 2/5$
windy	
$P(\text{true} p) = 3/9$	$P(\text{true} n) = 3/5$
$P(\text{false} p) = 6/9$	$P(\text{false} n) = 2/5$



# Play-tennis example: classifying X

- An unseen sample  $X = \langle \text{rain, hot, high, false} \rangle$

- $$P(X|p) \cdot P(p) =$$

$$P(\text{rain}|p) \cdot P(\text{hot}|p) \cdot P(\text{high}|p) \cdot P(\text{false}|p) \cdot P(p) = 3/9 \cdot 2/9 \cdot 3/9 \cdot 6/9 \cdot 9/14 = 0.010582$$

- $$P(X|n) \cdot P(n) =$$

$$P(\text{rain}|n) \cdot P(\text{hot}|n) \cdot P(\text{high}|n) \cdot P(\text{false}|n) \cdot P(n) = 2/5 \cdot 2/5 \cdot 4/5 \cdot 2/5 \cdot 5/14 = 0.018286$$

- Sample  $X$  is classified in class  $n$  (don't play)

<b>outlook</b>	
$P(\text{sunny} p) = 2/9$	$P(\text{sunny} n) = 3/5$
$P(\text{overcast} p) = 4/9$	$P(\text{overcast} n) = 0$
$P(\text{rain} p) = 3/9$	$P(\text{rain} n) = 2/5$
<b>temperature</b>	
$P(\text{hot} p) = 2/9$	$P(\text{hot} n) = 2/5$
$P(\text{mild} p) = 4/9$	$P(\text{mild} n) = 2/5$
$P(\text{cool} p) = 3/9$	$P(\text{cool} n) = 1/5$
<b>humidity</b>	
$P(\text{high} p) = 3/9$	$P(\text{high} n) = 4/5$
$P(\text{normal} p) = 6/9$	$P(\text{normal} n) = 2/5$
<b>windy</b>	
$P(\text{true} p) = 3/9$	$P(\text{true} n) = 3/5$
$P(\text{false} p) = 6/9$	$P(\text{false} n) = 2/5$

# Naïve Baye

---

- There's a lot of Maths/Calculations
- They are **all very simple calculations**
  - Counting
  - Multiplication
- Computers are **very good** at doing simple Maths/Calculations -> **Very fast**
  - **You will never have to do these calculations**
  - It's a tool for you to use
- Quick results
  - Although may not be the most accurate
  - Can be a **good starting point** -> **benchmark** other algorithms performance

# The Algorithms

Naive Bayes

Decision Trees

Random Forests

XGBoost

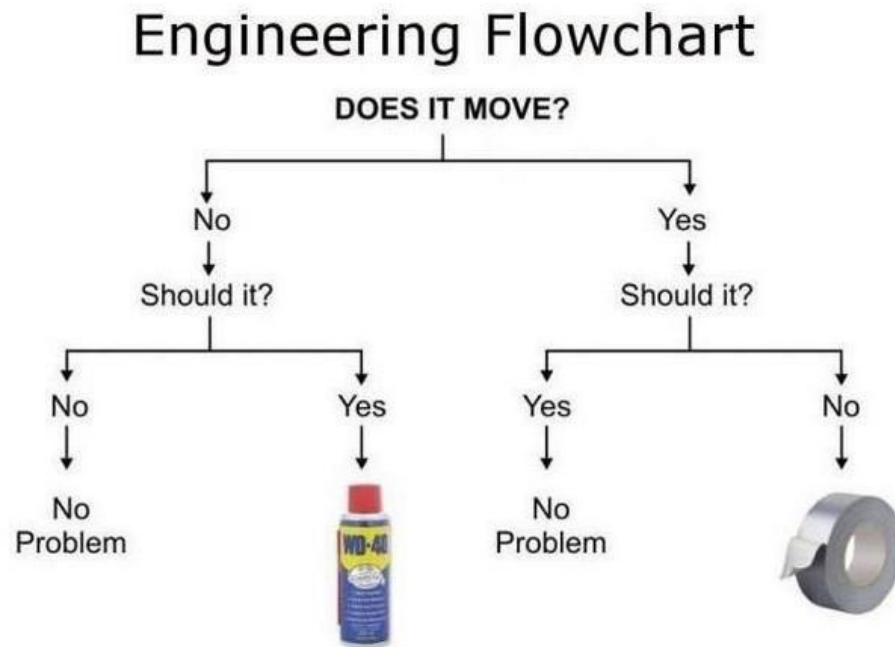
The image contains a vast amount of handwritten notes in physics and mathematics. Key sections include:

- Mechanics:**
  - Force diagrams on an inclined plane with equations like  $\sum F_y = 0 \Rightarrow F_n - mg \cos \theta = 0$  and  $F_n = mg \cos \theta$ .
  - Energy conservation:  $E_{pot, A} = 0$ ,  $E_{kin, A} = 0$ ,  $F = m \ddot{x} + 2F_s$ .
  - Velocity and acceleration:  $a = \frac{dv}{dt} = \frac{dv}{du} \frac{du}{dt}$ ,  $v = \sqrt{\frac{2(m_2 - m_1)gh}{(m_1 + m_2)}}$ .
  - Wave properties:  $v = \frac{\lambda}{T} = \lambda \omega$ ,  $\omega = 2\pi \nu$ ,  $k = \frac{2\pi}{\lambda}$ .
  - Spring-mass system:  $F = -k_F y$ ,  $F_G = mg \downarrow$ ,  $\sum F_y = may$ .
- Electromagnetism:**
  - Electric field:  $E_{in, A} = 0$ ,  $E_{end, E} = E_{med, A}$ .
  - Capacitors:  $C = \frac{Q}{U}$ ,  $U = \int \vec{E} \cdot d\vec{s}$ .
  - Resistor networks:  $U_{A, eff} = X_C \cdot I_{eff}$ .
- Optics:**
  - Snell's law:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$ .
  - Thin film interference:  $2d \cos \theta = m \lambda$ .
- Mathematics:**
  - Calculus:  $dE = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2}$ ,  $dE_x = \frac{2}{4\pi\epsilon_0} \frac{y dx}{r^3}$ .
  - Integration:  $E_n = n^2 \frac{h^2}{8md^2} = n^2 E_1$ .
  - Probability distributions:  $\Psi(x,0) = A \exp(-\frac{x^2}{2\sigma^2}) e^{i\phi}$ .

# Decision Tree

---

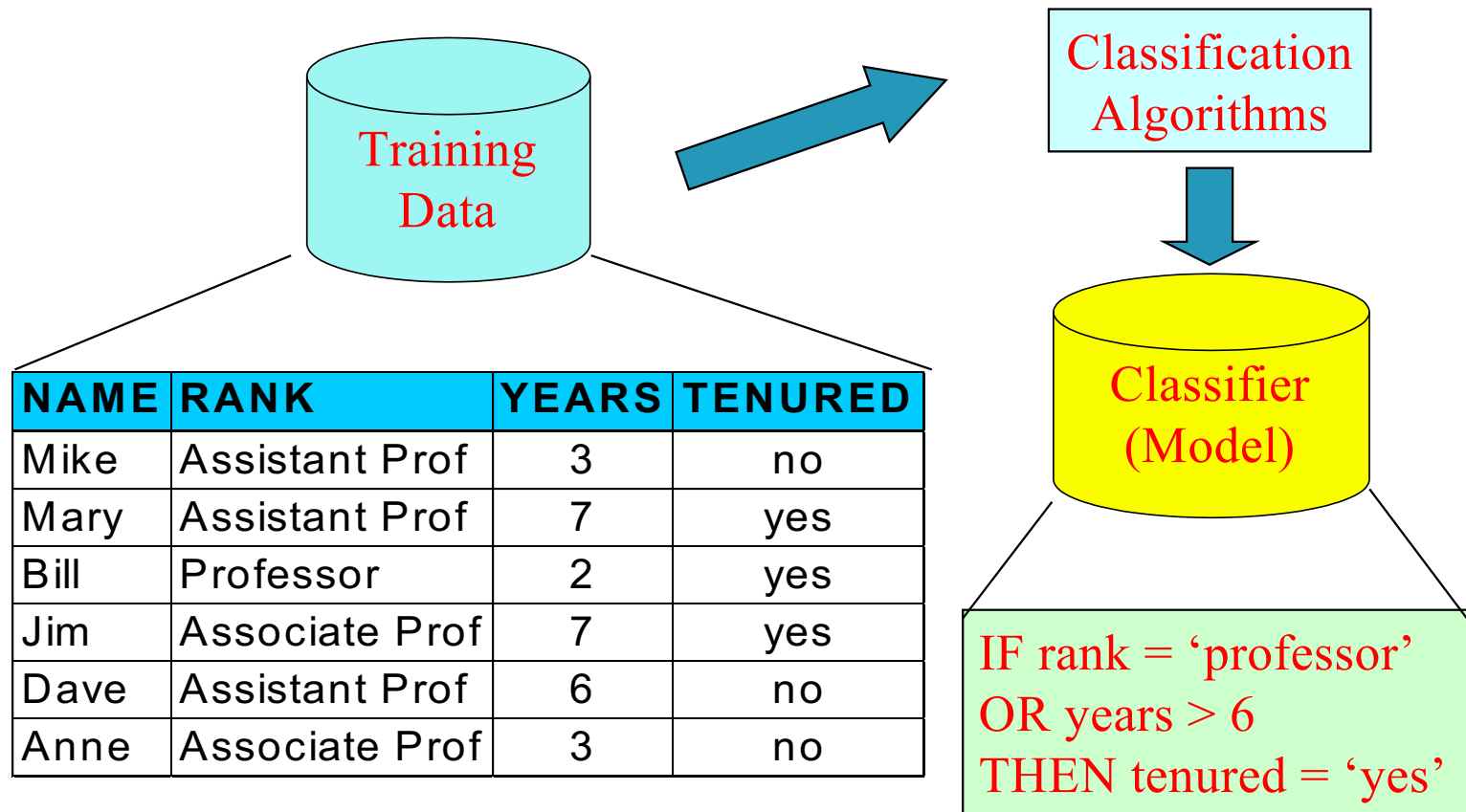
- Does it work for just this one time or can be used over time with different data?
  - Does it work in different situations ?
  - is a simplification or approximation of reality ? (George Box)



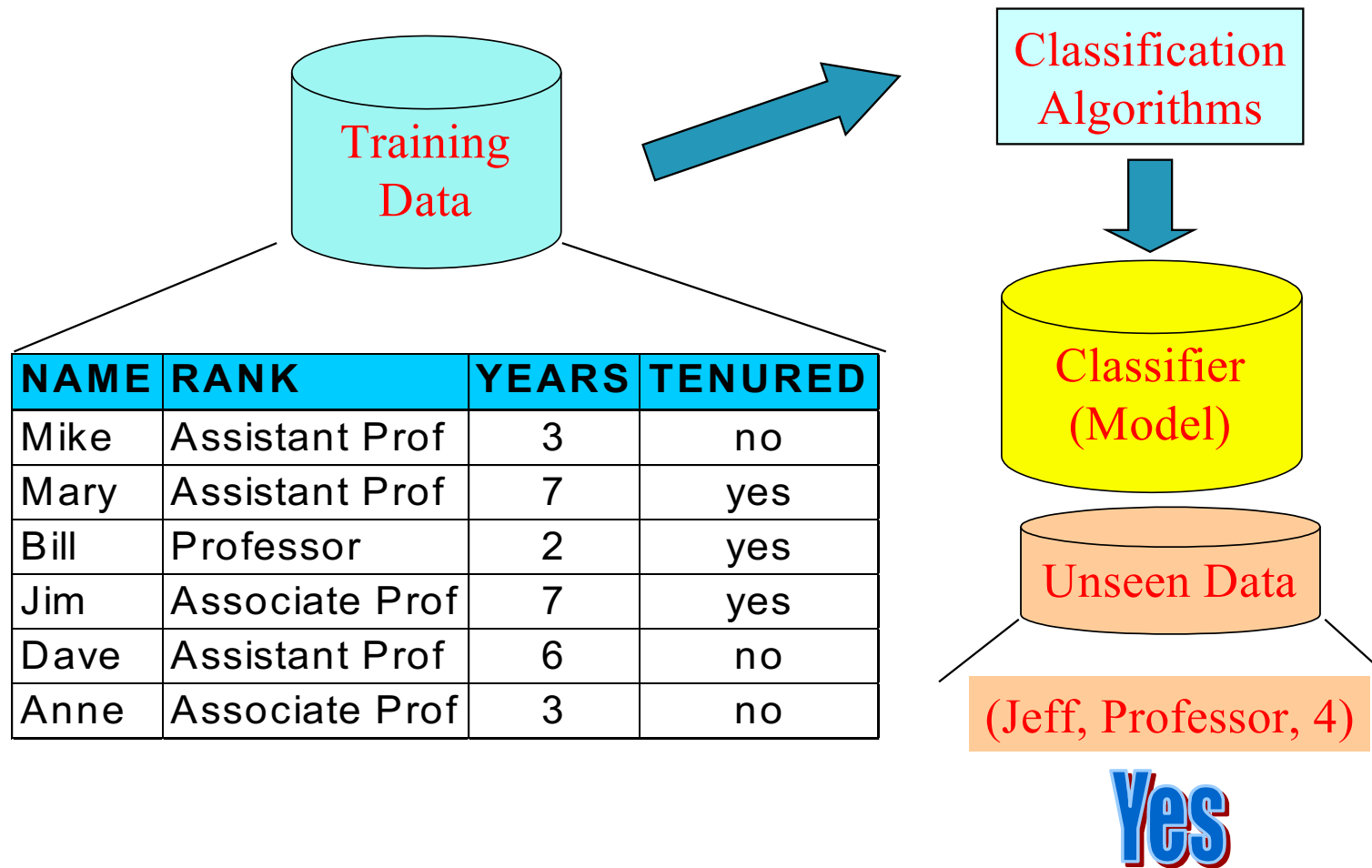
Decision Trees are :

- Simple
- Easy to understand
- Easy to explain
- Everyone can follow a DT
  
- IF-THEN statements
- Easy to code
- Easy to integrate into ...

# Classification Process (1): Model Construction



# Classification Process (1): Model Apply

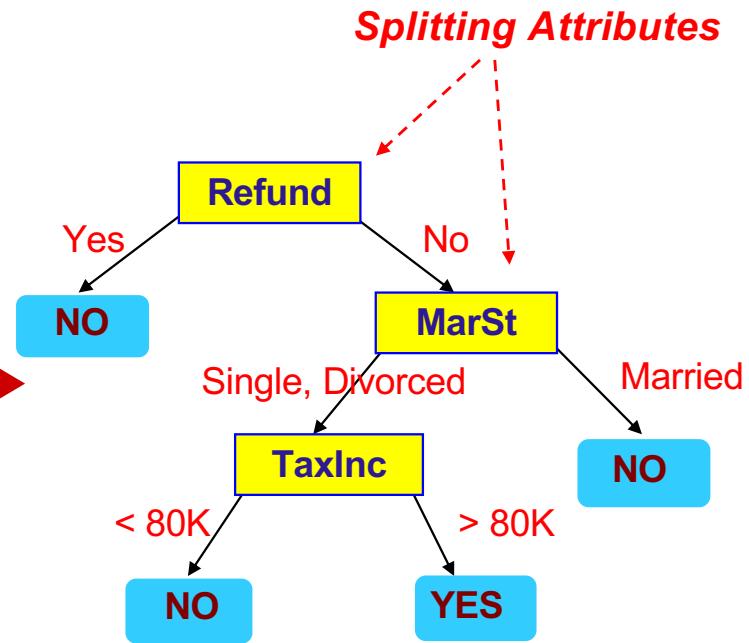


# Example of a Decision Tree

categorical      categorical      continuous      class

<i>Tid</i>	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

**Training Data**



**Model: Decision Tree**

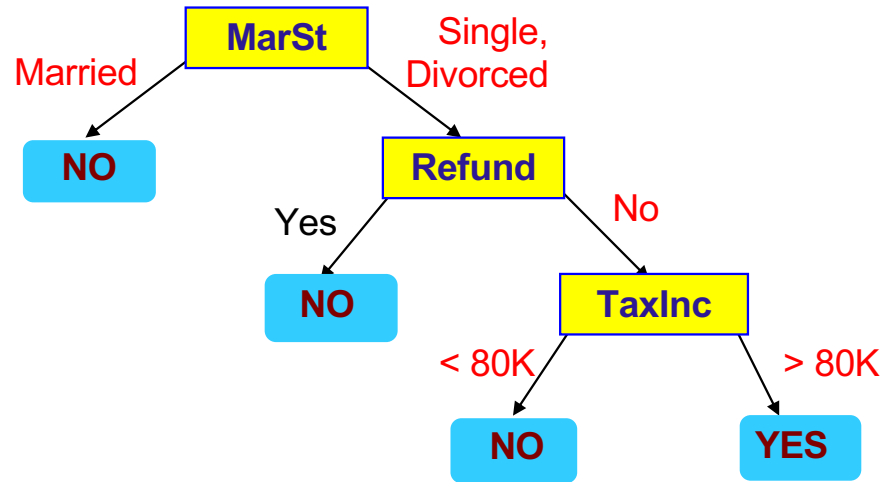
What attribute do we start with ?

This is called Information Gain

# Another Example of Decision Tree

categorical categorical continuous class

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes



There could be more than one tree that fits the same data!



# Algorithm for Decision Tree Induction

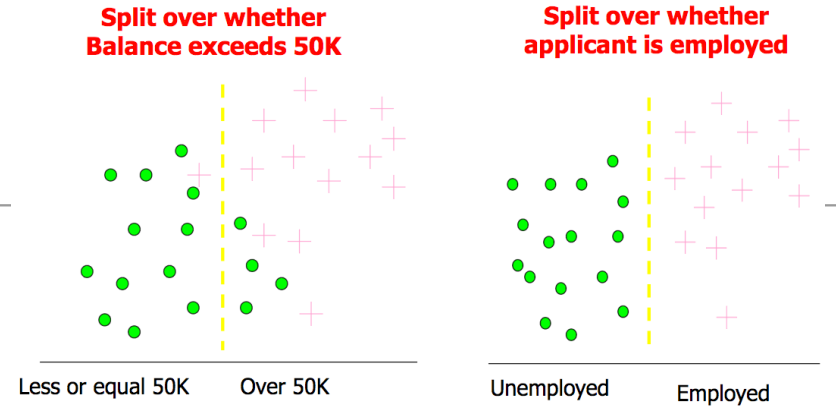
---

- Basic algorithm (a greedy algorithm)
  - Tree is constructed in a top-down recursive divide-and-conquer manner
  - At start, all the training examples are at the root
  - Attributes are categorical (if continuous-valued, they are discretized in advance)
  - Examples are partitioned recursively based on selected attributes
  - Test attributes are selected on the basis of a heuristic or statistical measure (e.g., information gain)
- Conditions for stopping partitioning
  - All samples for a given node belong to the same class
  - There are no remaining attributes for further partitioning – majority voting is employed for classifying the leaf
  - There are no samples left

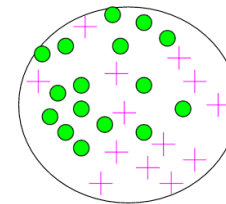
# How to split nodes/attributes

- Information Gain
  - Measures the level of impurity in a group of examples
  - We want to determine which attribute in a given set of training feature vectors is most useful for discriminating between the classes to be learned.
  - Information gain tells us how important a given attribute of the feature vectors is.

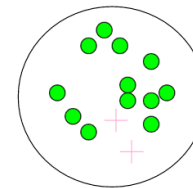
Which test is more informative?



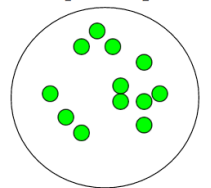
**Very impure group**



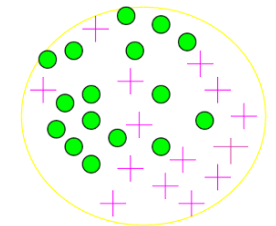
**Less impure**



**Minimum impurity**



• Entropy =  $\sum_i -p_i \log_2 p_i$




$p_i$  is the probability of class  $i$   
 Compute it as the proportion of class  $i$  in the set.

16/30 are green circles; 14/30 are pink crosses  
 $\log_2(16/30) = -.9$ ;  $\log_2(14/30) = -1.1$   
 Entropy =  $-(16/30)(-.9) - (14/30)(-1.1) = .99$

# Extracting Classification Rules from Trees

---

- Represent the knowledge in the form of **IF-THEN** rules
- One rule is created for each path from the root to a leaf
- Each attribute-value pair along a path forms a conjunction
- The leaf node holds the class prediction
- Rules are easier for humans to understand 

- Example

IF *age* = “<=30” AND *student* = “no” THEN *buys\_computer* = “no”

IF *age* = “<=30” AND *student* = “yes” THEN *buys\_computer* = “yes”

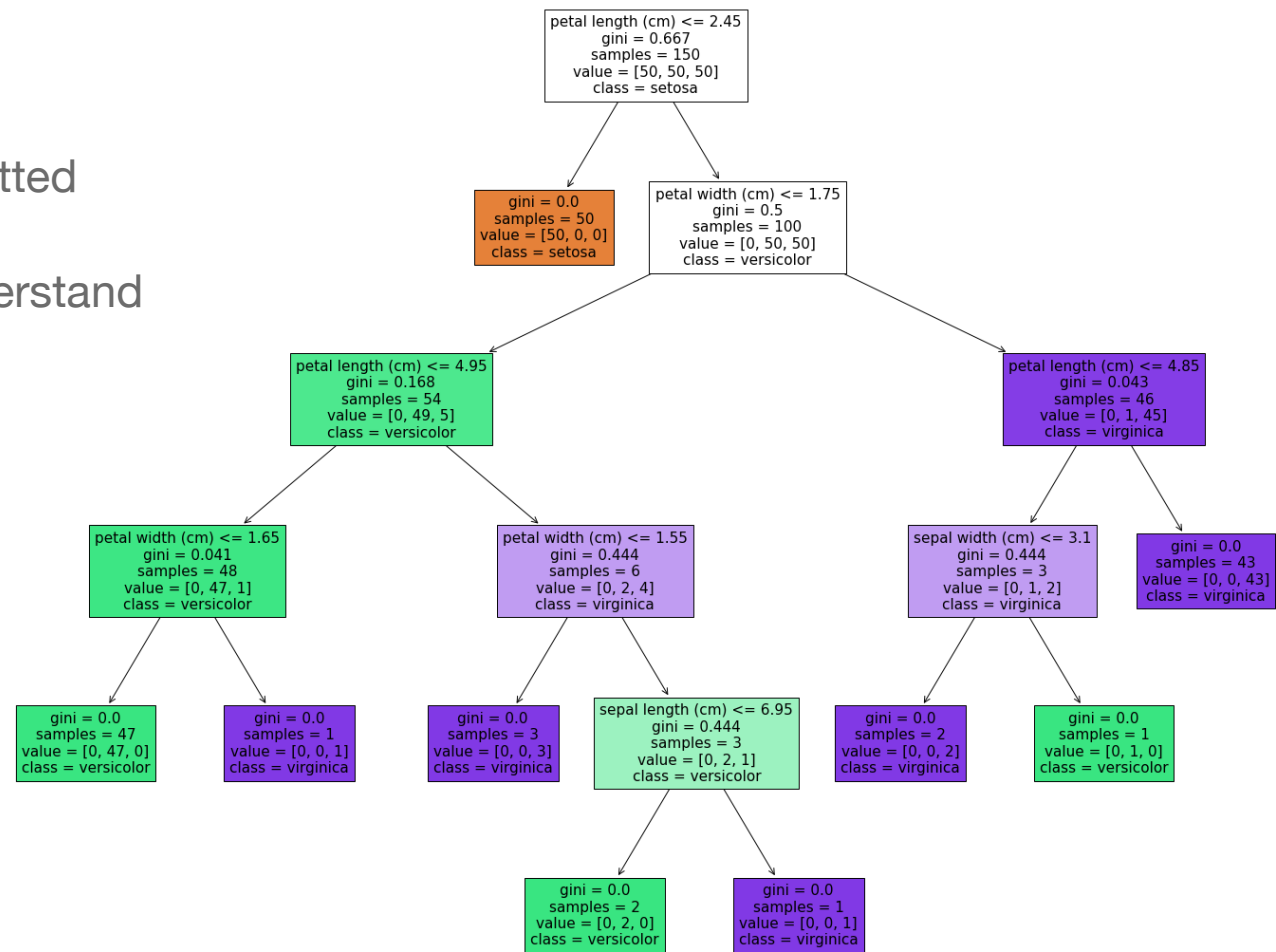
IF *age* = “31...40” THEN *buys\_computer* = “yes”

IF *age* = “>40” AND *credit\_rating* = “excellent” THEN *buys\_computer* = “yes”

IF *age* = “>40” AND *credit\_rating* = “fair” THEN *buys\_computer* = “no”

# Decision Tree Plot

- Depends on size of Decision Tree
- Small Decision Trees are can be plotted
- Large Tree becomes difficult to understand



# Decision Trees

---

- Form the basis for other algorithms
  - RandomForest
  - XGBoost
  
- Let's have a look at these

# The Algorithms

Naive Bayes

Decision Trees

Random Forests

XGBoost

The page contains a comprehensive set of handwritten physics notes, organized into several sections:

- Mechanics:**
  - Inclined Plane:** Shows a block on an inclined plane at angle  $\theta$ . Forces include normal force  $F_N$ , weight  $mg$ , and friction  $F_f$ . Equations include  $\sum F_y = 0 \Rightarrow F_N \cos \theta - mg = 0$  and  $F_f = \mu mg \cos \theta$ .
  - Pulleys:** Analyzes a system of two masses  $m_1$  and  $m_2$  connected by a string over a pulley. Derives acceleration  $a = \frac{m_2 - m_1}{m_1 + m_2} g$  and tension  $F = \frac{2m_1 m_2}{m_1 + m_2} g$ .
  - Energy:** Discusses potential energy  $E_{pot} = mgh$  and kinetic energy  $E_{kin} = \frac{1}{2}mv^2$ . Includes conservation of energy principles.
  - Projectile Motion:** Shows a projectile launched at angle  $\theta$  with initial velocity  $v_0$ . Derives horizontal range  $R = \frac{v_0^2 \sin(2\theta)}{g}$ .
- Electromagnetism:**
  - Electric Fields:** Derives the electric field  $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$  and potential  $V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$  for a point charge.
  - Capacitors:** Shows a parallel plate capacitor with area  $A$  and separation  $d$ . Derives capacitance  $C = \frac{\epsilon_0 A}{d}$  and energy stored  $U = \frac{1}{2} CV^2$ .
  - Resistors and Circuits:** Analyzes a circuit with resistors  $R$  and capacitors  $C$ . Discusses Ohm's law  $V = IR$  and Kirchhoff's laws.
- Waves:**
  - Wave Equation:** Shows a sinusoidal wave  $y(x,t) = A \sin(kx - \omega t + \phi)$ . Relates wavelength  $\lambda$ , frequency  $f$ , and wave speed  $v = \lambda f$ .
  - Interference:** Discusses path difference  $\Delta x$  and phase difference  $\Delta \phi$  for two waves.
- Optics:**
  - Thin Film Interference:** Shows a thin film of thickness  $t$  and refractive index  $n$  between two media. Derives conditions for constructive and destructive interference.
  - Lenses:** Analyzes a lens with focal length  $f$  and object distance  $s$ . Derives the lens equation  $\frac{1}{s} + \frac{1}{s'} = \frac{1}{f}$ .

# Random Forests

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- **Random forests**

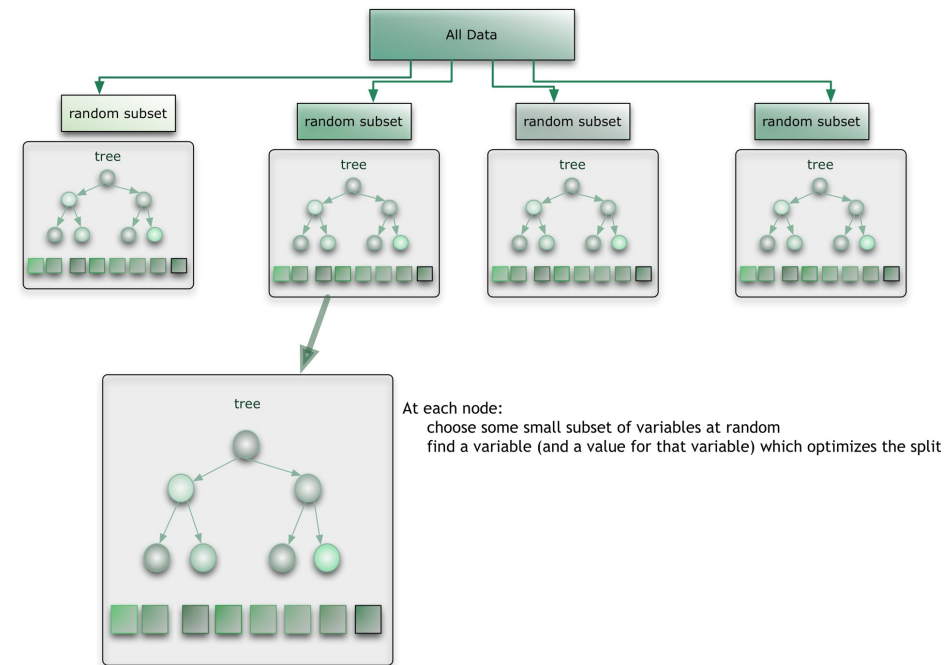
- are an **ensemble** learning method for classification, regression and other tasks, that operate by constructing **a multitude of decision trees** at training time and outputting the class that is the mode of the classes (classification) or mean prediction (regression) of the individual trees.

- Wisdom of Crowds



# Random Forests

- The Random Forest algorithm has three main features:
  - It uses a method called bagging, to create **different sub-sets of the original training data**.
  - It will **randomly** section different **subsets of the features/attributes** and build the decision tree based on this subset
  - By creating many different decision trees, based on different subsets of the training data and different subsets of the features, will **increase the probability of capturing all possible ways of modeling the data**.

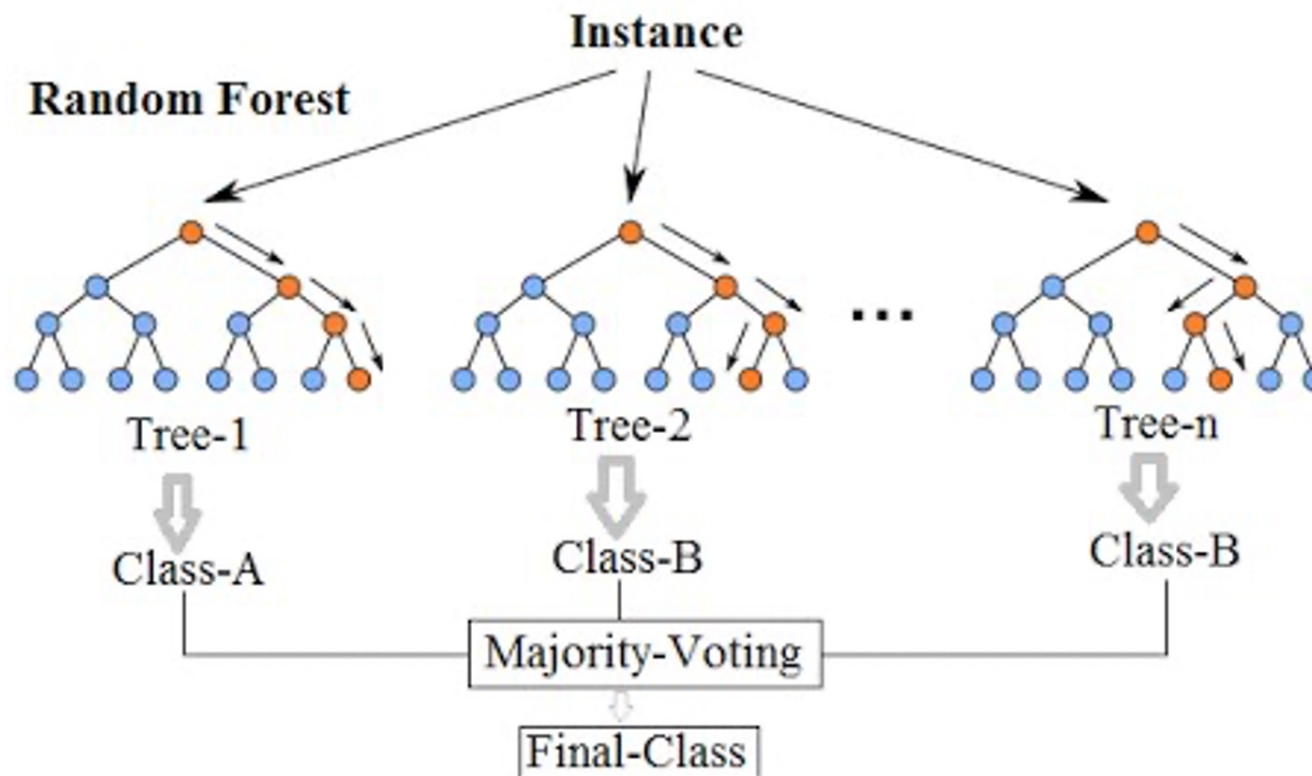




# Random Forests

---

## Random Forest Simplified



# The Algorithms

Naive Bayes

Decision Trees

Random Forests

XGBoost

The image contains a comprehensive set of handwritten physics and mathematics notes. Key sections include:

- Mechanics:**
  - Force diagrams on inclined planes with equations like  $\sum F_y = 0 \Rightarrow F_n - mg \cos \theta = 0$  and  $F_n = mg \cos \theta$ .
  - Energy conservation:  $E_{pot, A} = 0$ ,  $E_{kin, A} = 0$ ,  $F = m \cdot g \cdot \theta + 2F_s$ .
  - Wave motion:  $y(x,t) = A \sin(2\pi \frac{x}{\lambda} + \delta)$ ,  $y(x,t) = A \sin(kx - \omega t)$ ,  $2\pi v = k \omega = \frac{2\pi}{\lambda} v$ .
  - Spring systems:  $F = -k \cdot \Delta y$ ,  $\sum F_y = m a_y$ ,  $F_G = m g$ .
  - Rotational motion:  $\tau = r \times F$ ,  $F = F \sin \phi$ .
- Electromagnetism:**
  - Capacitors:  $C = \frac{Q}{U}$ ,  $U_A = X_C \cdot I$ .
  - Resistors:  $R = \frac{U}{I}$ .
  - Inductors:  $L = \frac{\Phi}{I}$ ,  $U_L = X_L \cdot I$ .
  - Electric fields:  $E = \frac{1}{4\pi \epsilon_0} \frac{q}{r^2}$ ,  $\oint \vec{E} \cdot d\vec{s} = \frac{Q_{enc}}{\epsilon_0}$ .
  - Magnetic fields:  $B = \mu_0 \cdot I$ ,  $\oint \vec{B} \cdot d\vec{s} = \mu_0 \cdot I_{enc}$ .
- Optics:**
  - Ray diagrams for lenses:  $\frac{1}{f} = \frac{1}{s} + \frac{1}{s'}$ .
  - Snell's Law:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$ .
  - Interference:  $\Delta x = \frac{\lambda}{2} \cdot \frac{d}{\lambda} \cdot \sin \theta$ .
- Mathematics:**
  - Calculus:  $dE = \frac{1}{4\pi \epsilon_0} \frac{dq}{r^2}$ ,  $dE_x = \frac{1}{4\pi \epsilon_0} \frac{dq}{r^2} \cos \theta$ .
  - Integration:  $E = \int dE$ ,  $\Phi = \int \vec{B} \cdot d\vec{A}$ .
  - Trigonometry:  $\sin^2 \theta = \frac{\lambda}{AB}$ ,  $\cos \theta = \frac{d}{r}$ .

# XGBoost

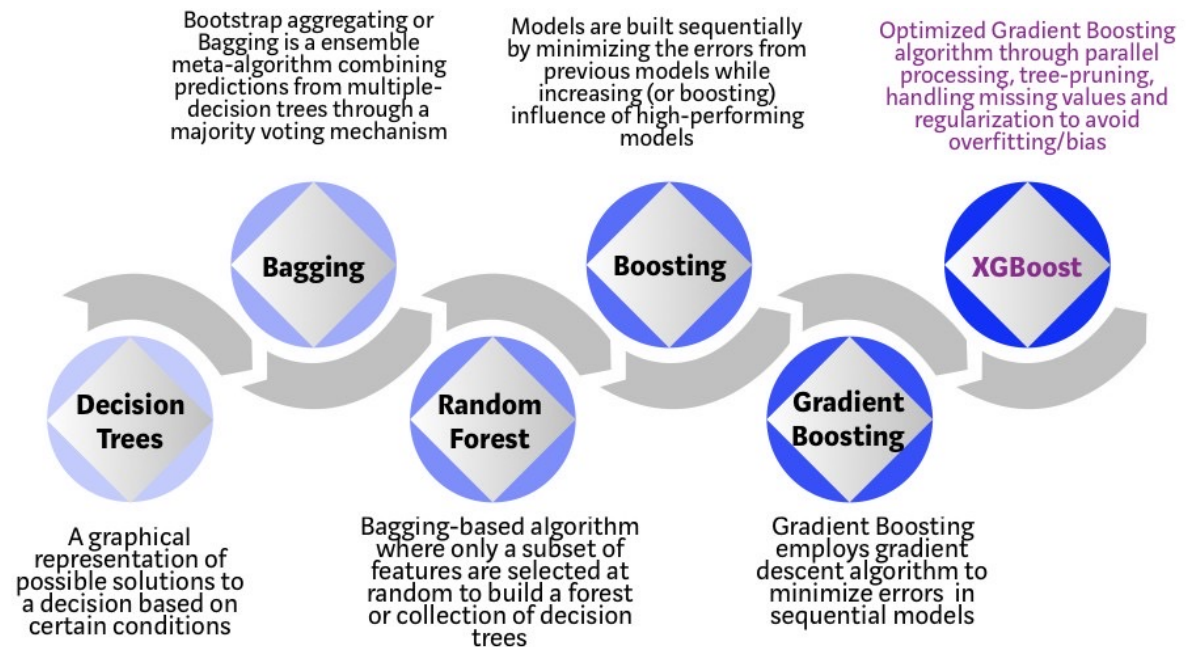
[Tianqi Chen and Carlos Guestrin original paper from 2016 – University of Washington](#)

## XGBoost: A Scalable Tree Boosting System

Can be used for

- Classification
- Regression
- Ranking problems

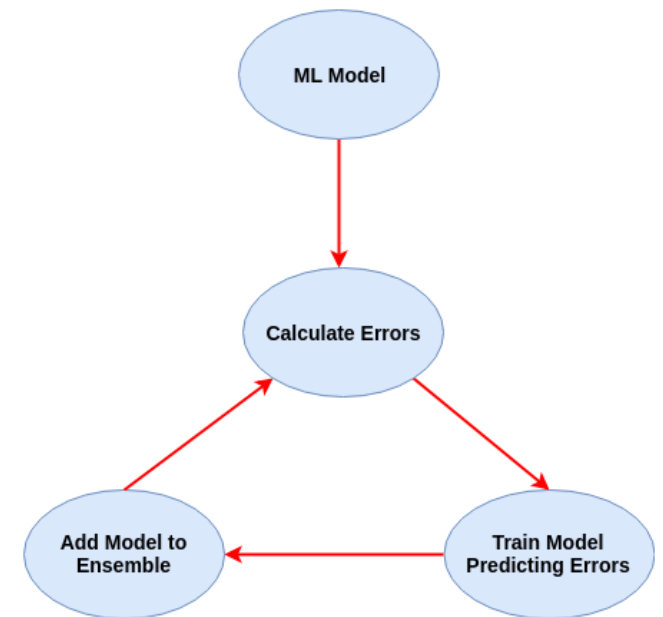
- Open Source Framework
- Kaggle Competitions
- Builds upon previous



# XGBoost

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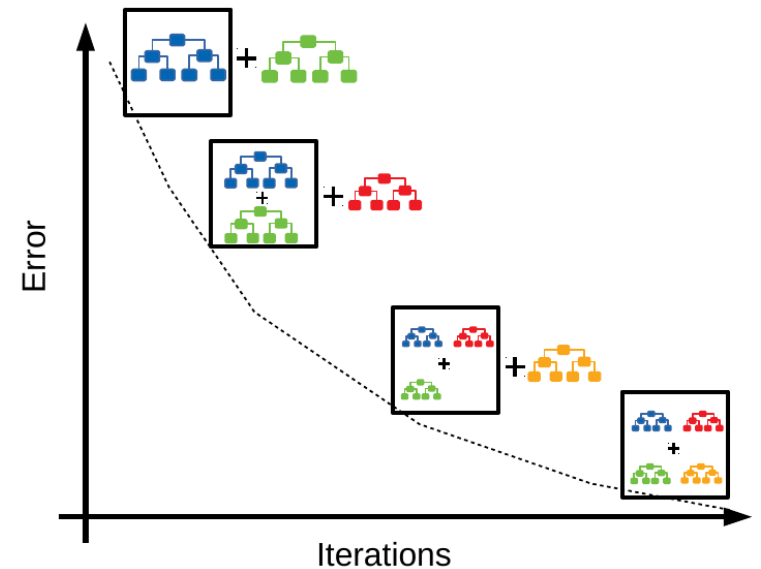
- Regular machine learning models, like a decision tree, simply train a single model on the dataset and use that for prediction.
- Building an ensemble, all the models are trained and applied to our data separately.
- **Boosting**, takes a more *iterative* approach. It's still technically an ensemble technique with many models are combined to perform the final prediction.
- Instead of training all the models in isolation of one another, **boosting trains models in succession**, with **each new model being trained to correct the errors made by the previous ones**.



# XGBoost

---

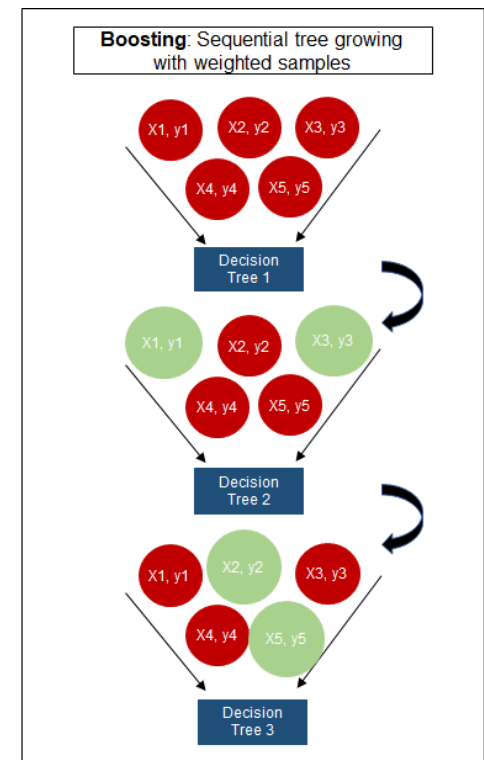
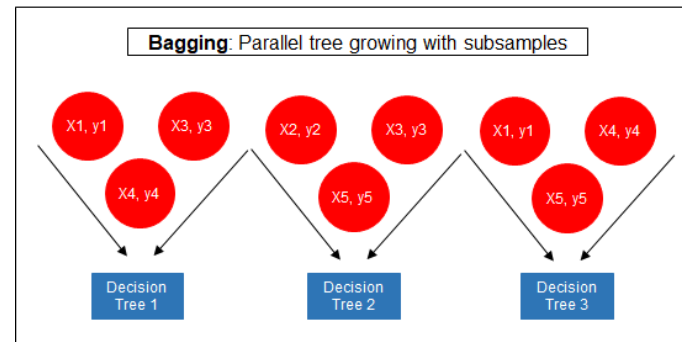
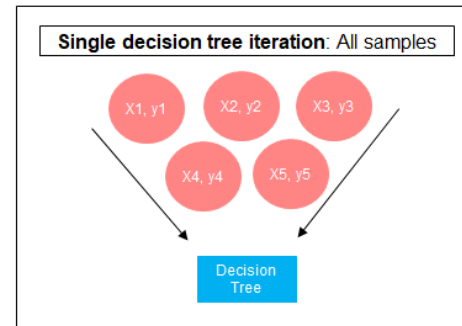
- Models are added sequentially until no further improvements can be made.
- Advantage is the new models being added are focused on **correcting the mistakes** which were caused by other models.
- Each subsequent model is trained on a **smaller portion** of data
  - **Quicker** to create each subsequent model
- In regular ensemble methods models are trained in isolation, all the models might end up making the same mistakes!
- **Gradient Boosting** specifically is an approach where new models are trained to predict the errors of prior models



# XGBoost

Optimised for

- Parallel processing
- Tree Pruning – Depth first approach
- Memory, Cache and Hardware optimised
- Fewer resources

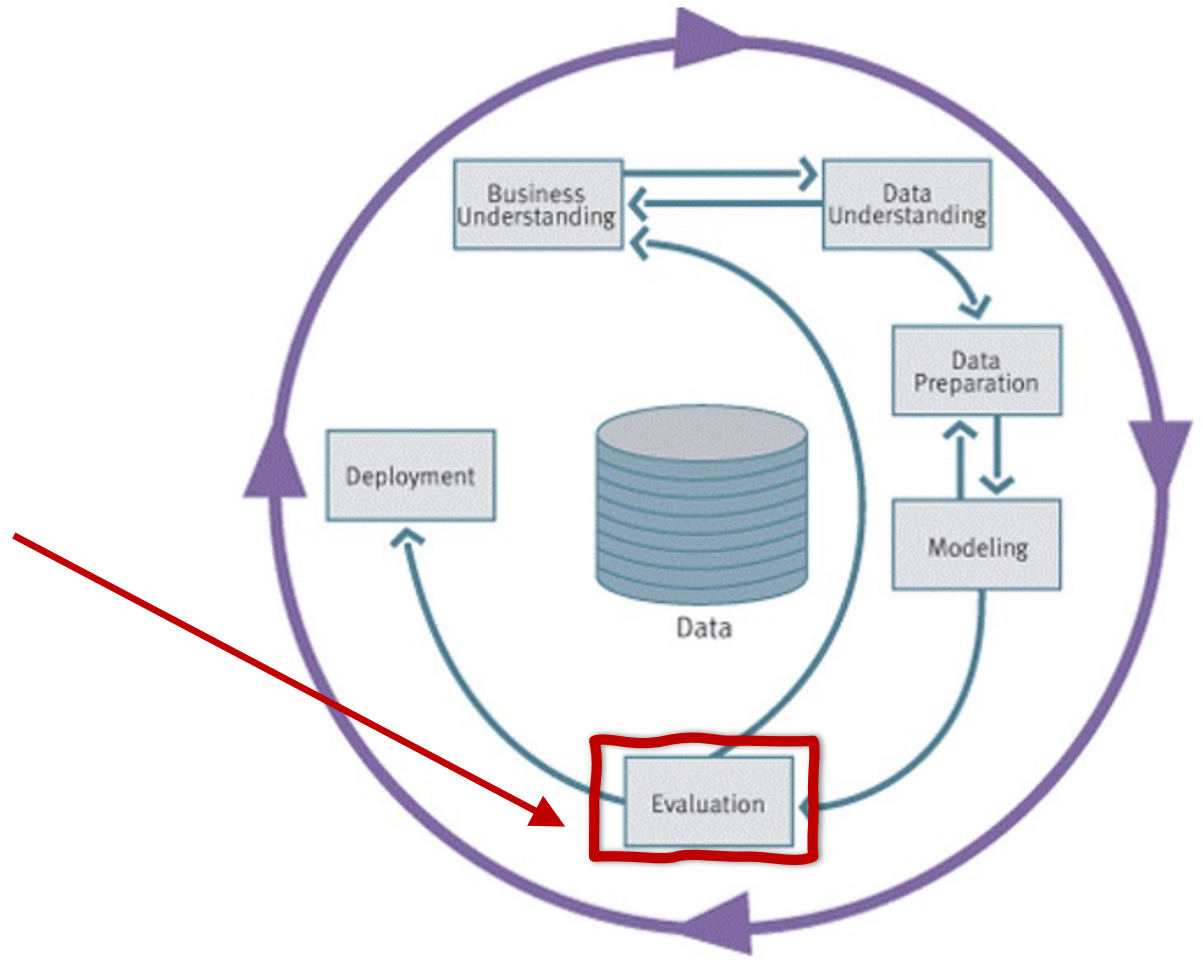


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# Test & Evaluate



Test & Evaluation





# Why do we evaluate?

---

- Why do we evaluate the models created?
  - Remember, we will create many models -> We need to find the one that works best
  - The one that works best, on our data (as it is now), for our problem, at this point in time
    - If we were to rerun all the code again with minor changes, we could get a different outcome
- What will work best for us
  - To determine which model is the most suitable for a task
  - To communicate to (business) users on what should be used

# How do we evaluate

---

- It isn't complicated – But many make it complicated
- It's very simple really!
- In reality it is just Counting
  - How many you **correctly predicted**
  - How many you **incorrectly predicted**
- Remember, a model **will/can never be 100% correct**
  - It is an approximation
- Keep It Simple!



# Classifier Accuracy

---

- The **accuracy** of a classifier on a given test set is the percentage of test set tuples that are correctly classified by the classifier
  - Often also referred to as **recognition rate**
  - **Error rate** (or **misclassification rate**) is the opposite of accuracy



## No Free Lunch

- In machine learning, there's something called the "No Free Lunch" theorem. In a nutshell, it states that no one algorithm works best for every problem.
- As a result, one should **try many different algorithms for the problem**, while using a hold-out "test set" of data to evaluate performance and select the winner.

# False Positives Vs False Negatives

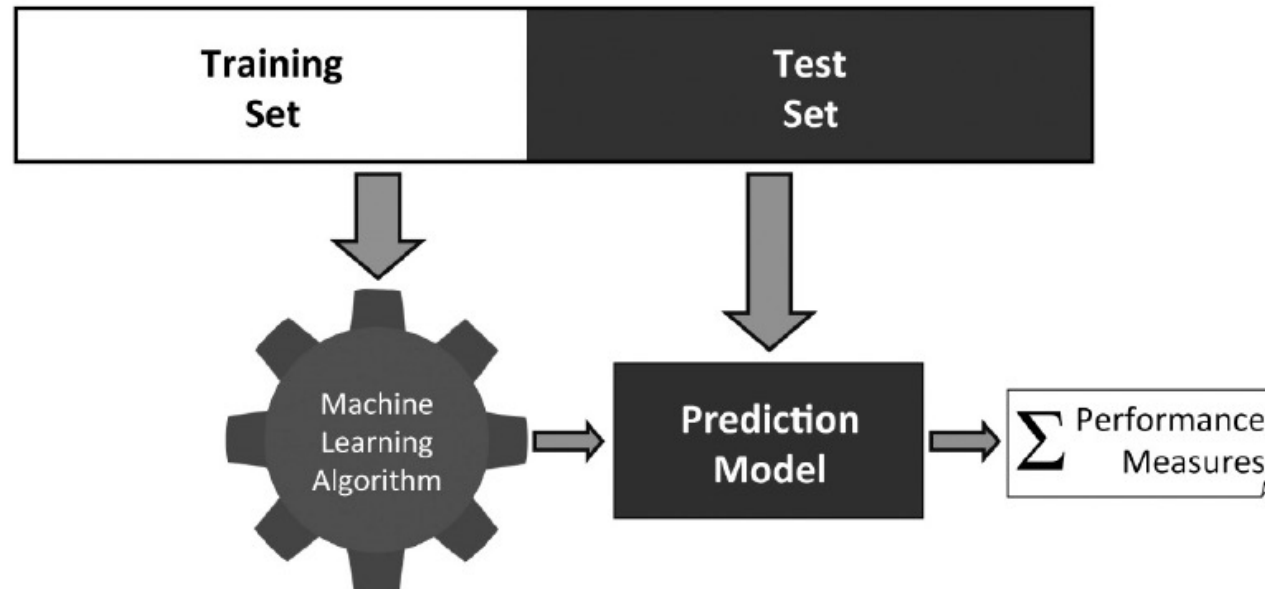
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- While it is useful to generate the simple accuracy of a classifier, sometimes we need more
- When is the classifier wrong?
  - **False positives** vs **false negatives**
  - Related to type I and type II errors in statistics
- Often there is a different cost associated with false positives and false negatives
  - Think about diagnosing diseases

# Test Dataset

---

- We run the model against the “unseen” dataset -> Test Dataset



The process of building and evaluating a model using a **hold-out test set**.

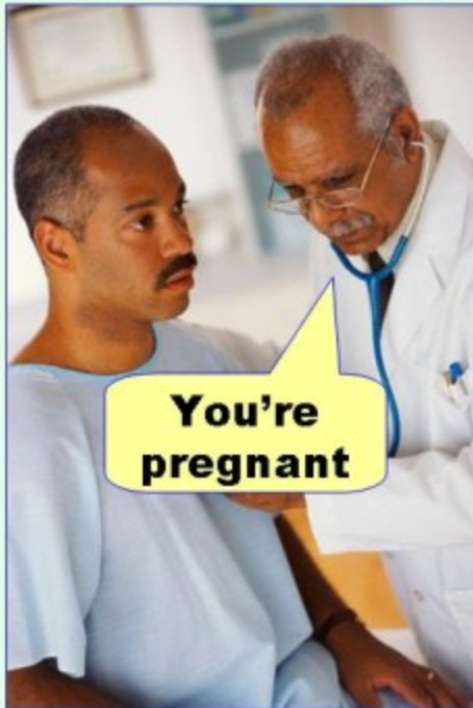
# Confusion Matrix

---

- **Confusion Matrix** used to illustrate how a classifier is performing in terms of false positives and false negatives
- Gives us more information than a single accuracy figure
- Allows us to think about the cost of mistakes
- Can be extended to any number of classes
  - Binary Classification
  - Multi-Class Classification

Classifier Result			Expected Result
Class A (yes)	Class B (no)		
✓	fn	Class A (yes)	
fp	✓	Class B (no)	

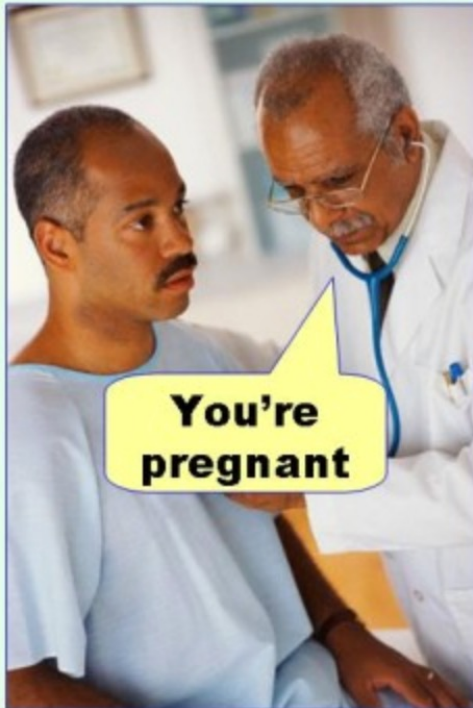
**Type I error**  
(false positive)



Type I  
&  
Type II  
Errors

"Type I" and "Type II" errors, names first given by Jerzy Neyman and Egon Pearson to describe rejecting a null hypothesis when it's true and accepting one when it's not, are too vague for stat newcomers (and in general). This is better. [\[via\]](#)

**Type I error**  
(false positive)



**Type II error**  
(false negative)



Type I  
&  
Type II  
Errors

"Type I" and "Type II" errors, names first given by Jerzy Neyman and Egon Pearson to describe rejecting a null hypothesis when it's true and accepting one when it's not, are too vague for stat newcomers (and in general). This is better. [\[via\]](#)



Lots of different versions of this.  
All are saying the same thing

	0 (condition negative)	1 (condition positive)	
0 (test outcome negative)	True Negative	False Negative (Type II Errors)	<b>Negative Prediction Rate =</b> $\frac{\sum \text{True Negative}}{\sum \text{Total Negative}}$
1 (test outcome positive)	False Positive (Type I Errors)	True Positive	<b>Precision = Positive Prediction Rate =</b> $\frac{\sum \text{True Positive}}{\sum \text{Total Positive}}$

<b>Negative Rate =</b> $\frac{\{\sum \text{False Negative} + \sum \text{False Positive}\}}{\sum \text{Total Population}}$	<b>True Negative Rate = Specificity =</b> $\frac{\sum \text{True Negative}}{\sum \text{All Negative}}$	<b>True Positive Rate = Sensitivity = Recall =</b> $\frac{\sum \text{True Positive}}{\sum \text{All Positive}}$	<b>Accuracy =</b> $\frac{\{\sum \text{True Negative} + \sum \text{True Positive}\}}{\sum \text{Total Population}}$
--	---	--	---

The attachment is not a virus  
& correctly predicted

The attachment is a virus  
But I've predicted it as not being a virus

	0 (condition negative)	1 (condition positive)	
0 (test outcome negative)	True Negative	False Negative (Type II Errors)	<b>Negative Prediction Rate =</b> $\frac{\sum \text{True Negative}}{\sum \text{Total Negative}}$
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The attachment is not a virus  
but is predicted as a virus

The attachment is a virus  
& correctly predicted

The customer does not commit fraud

The customer commits fraud  
But is predicted as not committing fraud

	0 (condition negative)	1 (condition positive)	
0 (test outcome negative)	True Negative	False Negative (Type II Errors)	<b>Negative Prediction Rate =</b> $\frac{\sum \text{True Negative}}{\sum \text{Total Negative}}$
1 (test outcome positive)	False Positive (Type I Errors)	True Positive	<b>Precision = Positive Prediction Rate =</b> $\frac{\sum \text{True Positive}}{\sum \text{Total Positive}}$
<b>Negative Rate =</b> $\frac{\{\sum \text{False Negative} + \sum \text{False Positive}\}}{\sum \text{Total Population}}$	<b>True Negative Rate = Specificity =</b> $\frac{\sum \text{True Negative}}{\sum \text{All Negative}}$	<b>True Positive Rate = Sensitivity = Recall =</b> $\frac{\sum \text{True Positive}}{\sum \text{All Positive}}$	<b>Accuracy =</b> $\frac{\{\sum \text{True Negative} + \sum \text{True Positive}\}}{\sum \text{Total Population}}$

The customer does not commit fraud  
but is predicted as committing fraud

The customer commits fraud

The patient does not have the condition

The patient does have the condition  
But we have predicted they don't

	0 (condition negative)	1 (condition positive)	
0 (test outcome negative)	True Negative	False Negative (Type II Errors)	<b>Negative Prediction Rate =</b> $\frac{\sum \text{True Negative}}{\sum \text{Total Negative}}$
1 (test outcome positive)	False Positive (Type I Errors)	True Positive	<b>Precision = Positive Prediction Rate =</b> $\frac{\sum \text{True Positive}}{\sum \text{Total Positive}}$
<b>Negative Rate =</b> $\frac{\{\sum \text{False Negative} + \sum \text{False Positive}\}}{\sum \text{Total Population}}$	<b>True Negative Rate = Specificity =</b> $\frac{\sum \text{True Negative}}{\sum \text{All Negative}}$	<b>True Positive Rate = Sensitivity = Recall =</b> $\frac{\sum \text{True Positive}}{\sum \text{All Positive}}$	<b>Accuracy =</b> $\frac{\{\sum \text{True Negative} + \sum \text{True Positive}\}}{\sum \text{Total Population}}$

The patient does not have the condition  
But we have predicted they have condition

The patient does have the condition

# Confusion Matrix - Example

---

A sample test set with model predictions.

ID	Target	Pred.	Outcome	ID	Target	Pred.	Outcome
1	spam	ham	FN	11	ham	ham	TN
2	spam	ham	FN	12	spam	ham	FN
3	ham	ham	TN	13	ham	ham	TN
4	spam	spam	TP	14	ham	ham	TN
5	ham	ham	TN	15	ham	ham	TN
6	spam	spam	TP	16	ham	ham	TN
7	ham	ham	TN	17	ham	spam	FP
8	spam	spam	TP	18	spam	spam	TP
9	spam	spam	TP	19	ham	ham	TN
10	spam	spam	TP	20	ham	spam	FP

		Prediction	
		'spam'	'ham'
Target	'spam'	6	3
	'ham'	2	9

# Confusion Matrix - Example

	0 (condition negative)	1 (condition positive)	
0 (test outcome negative)	True Negative	False Negative (Type II Errors)	<b>Negative Prediction Rate</b> = $\frac{\sum \text{True Negative}}{\sum \text{Total Negative}}$
1 (test outcome positive)	False Positive (Type I Errors)	True Positive	<b>Precision</b> = Positive Prediction Rate = $\frac{\sum \text{True Positive}}{\sum \text{Total Positive}}$

$$\text{precision} = \frac{6}{(6 + 2)} = 0.75$$

<b>Negative Rate</b> = $\frac{\{\sum \text{False Negative} + \sum \text{False Positive}\}}{\sum \text{Total Population}}$	<b>True Negative Rate</b> = <b>Specificity</b> = $\frac{\sum \text{True Negative}}{\sum \text{All Negative}}$	<b>True Positive Rate</b> = <b>Sensitivity</b> = <b>Recall</b> = $\frac{\sum \text{True Positive}}{\sum \text{All Positive}}$	<b>Accuracy</b> = $\frac{\{\sum \text{True Negative} + \sum \text{True Positive}\}}{\sum \text{Total Population}}$
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$$\text{misclassification accuracy} = \frac{(2 + 3)}{(6 + 9 + 2 + 3)} = 0.25$$

$$\text{classification accuracy} = \frac{(6 + 9)}{(6 + 9 + 2 + 3)} = 0.75$$

$$\text{recall} = \frac{6}{(6 + 3)} = 0.667$$

# Confusion Matrix – Example – What about Costs

---

- Not every outcome (or classification) has the same value
- A positive outcome could be worth money €
- A negative outcome could be work lots of money lost -€€€
- We can apply monetary values to the outcomes

Sample profit matrix for a credit scoring problem.

		Prediction	
		'good'	'bad'
Target	'good'	140	-140
	'bad'	-700	0

It was predicted as a "Good" Risk  
But in reality it turned out to be "Bad".  
In this case, how much on average would such a scenario cost us

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We should have approved these.  
But we didn't.  
Missed opportunity cost

We will do nothing with these.  
So no cost/€

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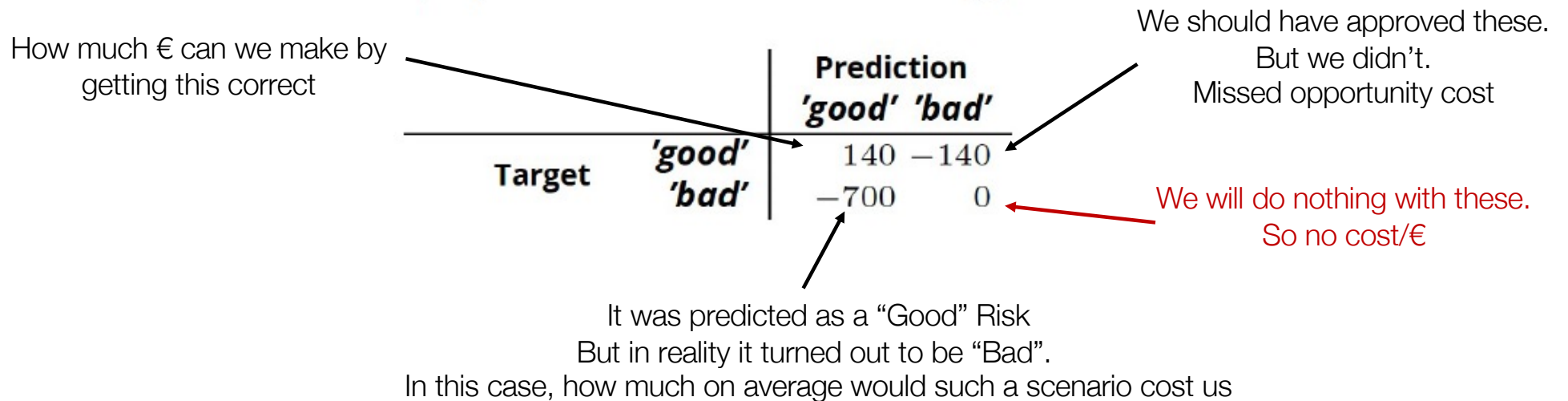
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# Confusion Matrix – Example – What about Costs

---

- Add up the numbers from each part/box of the Confusion Matrix
  - Total = € **potential** value for model
- Accountants like to see these numbers
- Your managers like to see these numbers
- Bosses like to see these numbers
- It quantifies/costs the **potential** € for each model
- The Business will understand using € (Language of Business)
  - Vs using Numbers + Percentages + Unusual Terms (Language of Analysts, Machine Learning, etc )

# Hold-Out Testing Sets

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- Split the available data into a *training set* and a *test set*

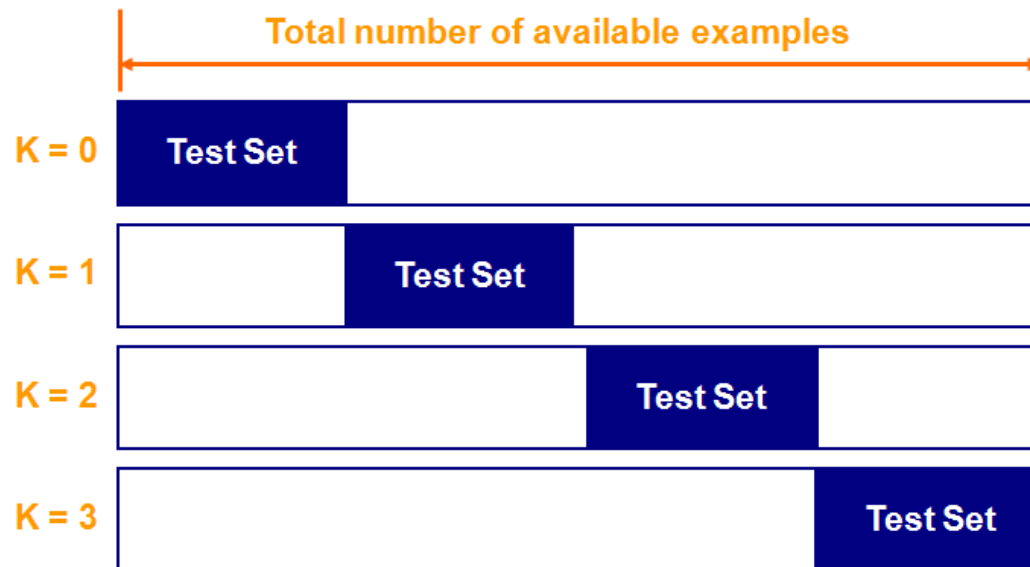


- Train the classifier in the training set and evaluate based on the test set
- A couple of drawbacks
  - We may not have enough data
  - We may happen upon an *unfortunate split*

# K-Fold Cross Validation

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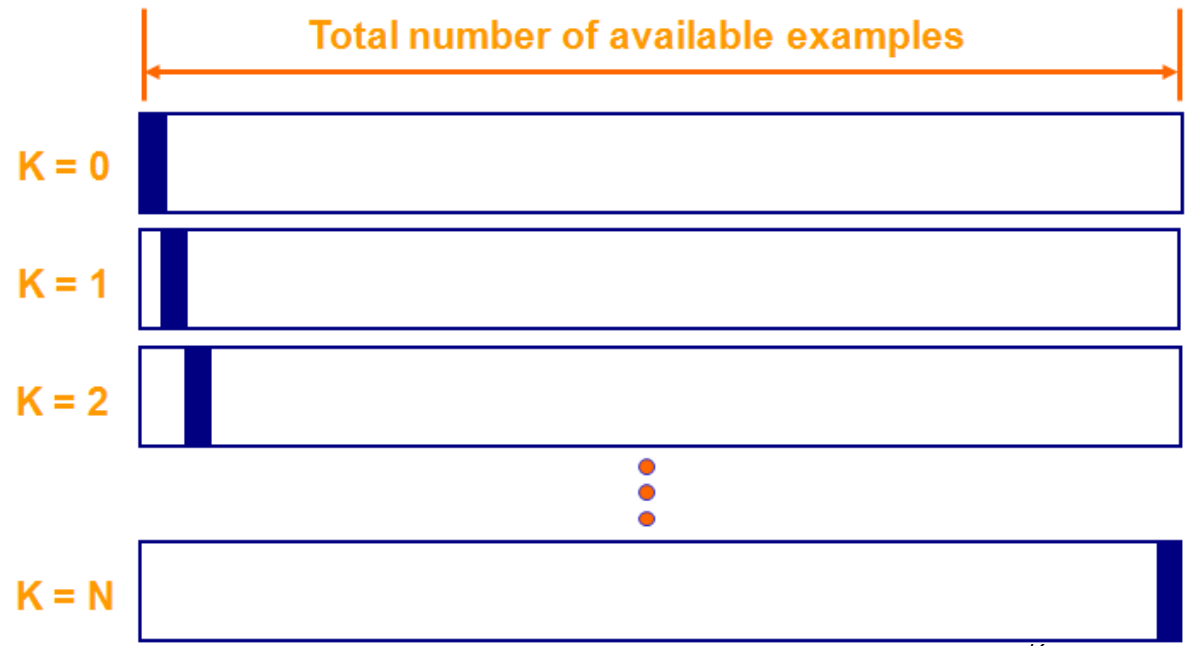
- An alternate is to divide the dataset into smaller chunks (Train & Test)
- $k$  *folds* – where  $k$  is the number of times to divide the data
- For each of  $k$  experiments, use  $k^{\text{th}}$  fold for testing and everything else for training
- Average the results across the  $k$  folds



# K-Fold Cross Validation

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- The accuracy of the system is calculated as the average error across the k folds
- The main advantages of k-fold cross validation are that every example is used in testing at some stage and the problem of an *unfortunate split* is avoided
- Any value can be used for k
  - 10 is most common
  - Depends on the data set



## A lot covered

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- We have covered a lot in this class
- What is Classification
- Different Algorithms
- How to Evaluate
  
- **Keep It Simple!**
- Lab Work
  - Examples of the Algorithms
  - Examples of Evaluation
  - A few lines of code
  
- Next week we will
  - Look at a few more algorithms
  - Go over the Evaluate steps again





Time for an  
Example



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Any Questions ?

What Now/Next ?